A High-Efficiency Grid-Tie
Battery Energy Storage System

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ABSTRACT

Lithium-ion based battery energy storage system has become one of the most popular forms of energy storage system for its high charge and discharge efficiency and high energy density. This dissertation proposes a high-efficiency grid-tie lithium-ion battery based energy storage system, which consists of a LiFePO4 battery based energy storage and associated battery management system (BMS), a high-efficiency bidirectional ac-dc converter and the central control unit which controls the operation mode and grid interface of the energy storage system. The BMS estimates the state of charge (SOC) and state of health (SOH) of each battery cell in the pack and applies active charge equalization to balance the charge of all the cells in the pack. The bidirectional ac-dc converter works as the interface between the battery pack and the ac grid, which needs to meet the requirements of bidirectional power flow capability and to ensure high power factor and low THD as well as to regulate the dc side power regulation.

A highly efficient dual-buck converter based bidirectional ac-dc converter is proposed. The implemented converter efficiency peaks at 97.8% at 50-kHz switching frequency for both rectifier and inverter modes. To better utilize the dc bus voltage and eliminate the two dc bus bulk capacitors in the conventional dual-buck converter, a novel bidirectional ac-dc converter is proposed by replacing the capacitor leg of the dual-buck converter based single-phase bidirectional ac-dc converter with a half-bridge switch leg. Based on the single-phase bidirectional ac-dc converter topology, three novel three-phase bidirectional ac-dc converter topologies are proposed.

In order to control the bidirectional power flow and at the same time stabilize the system in mode transition, an admittance compensator along with a quasi-proportional-
resonant (QPR) controller is adopted to allow smooth startup and elimination of the steady-state error over the entire load range. The proposed QPR controller is designed and implemented with a digital controller. The entire system has been simulated in both PSIM and Simulink and verified with hardware experiments. Small transient currents are observed with the power transferred from rectifier mode to inverter mode at peak current point and also from inverter mode to rectifier mode at peak current point.

The designed BMS monitors and reports all battery cells parameters in the pack and estimates the SOC of each battery cell by using the Coulomb counting plus an accurate open-circuit voltage model. The SOC information is then used to control the isolated bidirectional dc-dc converter based active cell balancing circuits to mitigate the mismatch among the series connected cells. Using the proposed SOC balancing technique, the entire battery storage system has demonstrated more capacity than the system without SOC balancing.
To my parents

Genrong Qian and Youzhu Xu

To my wife and son

Yanfei Shen and Siyuan Qian
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Chapter 1 Introduction

1.1 Background

With the increased concerns on environment and cost of energy, more renewable energy sources are integrated into the power grid in the form of distributed generation (DG). California has mandated that 20% of its power come from renewables by 2010 and 33% by 2020. Many other states and countries have similar regulations. The renewable energy source based DG systems are normally interfaced to the grid through power electronic converters and energy storage systems. A systematic organization of these DG systems, energy storage systems, and a cluster of loads forms a microgrid. The microgrid not only has the inherited advantages of single DG system but also offers more control flexibilities to fulfill system reliability and power quality requirement with proper management and control [1]-[6].

Rather than using fossil fuel, energy storage such as battery or ultra-capacitor systems can be used to provide fast frequency regulation, load following and ramping services when the DGs are integrated into the power grid [7]-[17]. Recent developments in lithium-ion battery technology show many advantages compared to lead-acid batteries and nickel-metal hydride batteries, such as high power and energy density, high working cell voltage, low self-discharge rate and high charge-discharge efficiency [18]-[22].

As shown in Figure 1.1, the energy storage system consists of three subsystems, a LiFePO4 battery pack and associated battery management system (BMS), a bidirectional ac-dc converter, and the central control unit which controls the operation mode and grid interface of the energy storage system. The BMS controller monitors the parameters of each battery cell, such as cell voltage, temperature, charge and discharge current; estimates the state of charge (SOC) and state of health (SOH) of each battery cell in the pack. The SOC information is then used to control the charge equalization circuits to mitigate the mismatch among the series connected battery cells. The SOC and SOH information is also used by the central control unit to determine the operating mode of the
energy storage system. The bidirectional ac-dc converter works as the interface between the battery pack and the ac grid, which needs to meet the requirements of bidirectional power flow capability and to ensure high power factor and low THD as well as regulate the dc side power regulation.

![Diagram](image)

**Figure 1.1 Simplified diagram of the lithium-ion battery energy storage system**

In this dissertation, a background description and review of the state-of-the-art BMS and bidirectional ac-dc converters [23]-[26] are presented firstly to define this work and its novelty. Then, the challenges will be identified related to the design and control issues in the present battery energy storage systems. The high-efficiency bidirectional ac-dc converter in the dissertation clearly demonstrated the feasibility of bidirectional power flow capability with the proposed control method [27]-[29]. Detailed operating modes and energy transfer mechanism have been described. To better utilize the dc bus voltage and eliminate the two dc bus capacitors, a novel bidirectional ac-dc converter is proposed by replacing the two-capacitor leg of the dual-buck converter based single-phase bidirectional ac-dc converter with a two-switch leg. To further reduce the size of the inductors, several novel topologies with optimized magnetic integration are proposed.
Experimental results have demonstrated that the proposed high-efficiency battery energy storage system effectively mitigates the mismatch among the series connected cells and support reactive power flow and seamless energy transfer.

1.2 State-of-the-art Battery Management System

1.2.1 Introduction to Battery Management System

In a lithium-ion battery system, BMS is the key component to ensure all cell voltages being strictly kept in boundaries for safety operation and cycle life. There are two key functions of the BMS in this work – monitoring and charge equalization.

First, the BMS monitors the status of all the series connected lithium-ion battery cells in the system. The parameters being monitored include cell voltage, cell temperature, charging or discharging current. The voltage, current and temperature information are then processed by the BMS controller to determine the SOC, SOH and capacity of each battery cell.

Second, the BMS applies active balancing to equalize the charge of the cells in the pack and to ensure all the cells operating in the designed SOC range. Due to production deviations, inhomogeneous aging, and temperature difference within the battery pack, there are SOCs or capacities imbalances between battery cells. Minimizing the mismatches across all the cells is important to guarantee the power or energy performance of the pack.

1.2.2 SOC Estimation

SOC is a measure of the amount of electrochemical energy left in a cell or battery. It is expressed as a percentage of the battery capacity and indicates how much charge (energy) stored in an energy storage element. It has been a long-standing challenge for battery industry to precisely estimate the SOC of lithium-ion batteries. The electrochemical reaction inside batteries is very complicated and hard to model electrically in a reasonably accurate way. So far, the state-of-the-art SOC accuracy for electric vehicle/plug-in hybrid EV (EV/PHEV) applications is in the range of 5%-10% [30]-[33].
Table 1.1 shows the comparison of different SOC estimation schemes. Among all the practical techniques, the Coulomb counting plus an accurate open-circuit voltage model is the algorithm being used here to estimate the SOC for its high accuracy with a relatively simple implementation.

<table>
<thead>
<tr>
<th>Technique</th>
<th>Summarized Features</th>
<th>Pros</th>
<th>Cons</th>
</tr>
</thead>
<tbody>
<tr>
<td>Discharge</td>
<td>Discharge with DC current and measure time to a certain threshold</td>
<td>Most accurate</td>
<td>Offline Time and energy consuming</td>
</tr>
<tr>
<td>Coulomb counting</td>
<td>Counting charges that have been injected/pumped out of battery</td>
<td>Online Easy</td>
<td>Loss model Need accuracy</td>
</tr>
<tr>
<td>Open circuit voltage</td>
<td>VOC-SOC look-up table</td>
<td>Online Accurate</td>
<td>Time consuming</td>
</tr>
<tr>
<td>Artificial neural network</td>
<td>Adaptive artificial neural network system</td>
<td>Online</td>
<td>Training data needed</td>
</tr>
<tr>
<td>Impedance</td>
<td>Impedance of the battery (RC combination)</td>
<td>Online SOC and SOH</td>
<td>Cost Temp-sensitive</td>
</tr>
<tr>
<td>DC resistance</td>
<td>$R_{dc}$</td>
<td>Online Easy</td>
<td>Cost Temp-sensitive</td>
</tr>
<tr>
<td>Kalman filter</td>
<td>Get accurate information out of inaccurate data using Kalman filter</td>
<td>Online Dynamic</td>
<td>Large computing Model needed</td>
</tr>
</tbody>
</table>

1.2.3 Charge Equalization

Due to inevitable differences in chemical and electrical characteristics from manufacturing, aging, and ambient temperatures, there are SOC or capacity imbalances between battery cells. When these unbalanced batteries are left in use without any control, such as cell equalization, the energy storage capacity decreases severely. Thus, charge
equalization for a series connected battery string is necessary to minimize the mismatches across all the cells and extend the battery lifecycle.

**Figure 1.2 Classification of conventional charge equalization methods**

Charge balancing methods can be classified into two categories: active and passive [34]-[40]. Active cell balancing helps balance the cells in a battery module to maintain the same voltage or SOC by monitoring and injecting appropriate balancing current into individual battery cell based on the balancing scheme. Compared with the traditional passive cell balancing approach, the active cell balancing offers the advantage of high system efficiency and fast balancing time. As shown in Figure 1.2, the active cell balancing method can be divided into two groups: unidirectional and bidirectional cell balancing. Among these schemes, multiple-winding transformer-based solutions are attractive for their effective low-cost equalization. However, it is difficult to implement multiple windings in a single transformer when the lithium-ion battery string consists of more than 100 cells in electric vehicle (EV) application. The switched capacitor-based solution is also not considered for the long equalization time. A modularized charge equalizer based on switched transformer and bidirectional dc-dc converter schemes is employed in this dissertation. The isolated bidirectional dc-dc converter regulates from the 12-cell battery stack voltage to each individual cell voltage. The average current-mode control is employed such that the average inductor current is regulated to the command current, which is set by the active cell-balancing control algorithm.
1.3 State-of-the-art Bidirectional AC-DC Converter

1.3.1 Introduction to Bidirectional AC-DC Converter

Traditionally, full-wave diode bridge or thyristor converters were employed to synthesize dc voltage from the ac grid. These rectifiers pollute the grid with undesired input ac current harmonics. Ac-dc converters with pulse width modulation (PWM) are employed to increase power factor and reduce current harmonics.

![Diagram of bidirectional power flow](image)

**Figure 1.3 Illustration of bidirectional power flow**

In a battery energy storage system, a bidirectional ac-dc converter with a proper charging-discharging profile is required to transfer energy between the battery pack and the ac grid. An ac-dc converter with bidirectional power flow capability is shown in Figure 1.3, where $P_{ac}$ is defined as the active power that ac side receives and $P_{dc}$ is defined as the power that dc side receives. The converter works as a rectifier when the power is transferred from ac grid to dc sources ($P_{ac} < 0$ and $P_{dc} > 0$). Alternately, it works as an inverter when the power is transferred from dc sources to ac grid ($P_{ac} > 0$ and $P_{dc} < 0$).

To realize bidirectional power flow in ac-dc converters, the power switch should carry the current in both directions. It is usually implemented with the power Metal-Oxide-
Semiconductor-Field-Effect-Transistor (MOSFET) or the Insulated-Gate Bipolar-Transistor (IGBT) in parallel with a diode.

### 1.3.2 Single-Phase Bidirectional AC-DC Converter

Various topologies that are capable of running with bidirectional power flow have been proposed [41]-[53]. Basically they are divided into two types: non-isolated and isolated converters, meeting different application requirements. The high-frequency transformer based system is an attractive solution to obtain isolation between ac grid and dc source. However, the non-isolated converters are more attractive because these systems are lower in cost and more efficient.

![Circuit diagram of a single-phase four-switch bidirectional ac-dc converter](image)

**Figure 1.4 Circuit diagram of a single-phase four-switch bidirectional ac-dc converter**

For the single-phase converter, the commonly used bidirectional converter topology consists of four power switches as shown in Figure 1.4. For this topology, the power MOSFET cannot be used as the main switch in the high-voltage high-power applications because the intrinsic MOSFET body diode conduction could cause device failure. The IGBT can be used as the main switch for the single-phase converter. However, an IGBT has higher switching and conduction losses compared with a power MOSFET. Also the IGBT only allows operating at a lower switching frequency than the power MOSFET allows, thus resulting in a larger filter size.
As shown in Figure 1.5, the high-efficiency bidirectional ac-dc converter in the dissertation adopts opposed current half bridge inverter architecture [23]. Since it consists of two buck converters and also has features of the conventional half bridge inverter, it is named as dual-buck half bridge inverter [24]-[26]. By using MOSFET device, not only can the switching loss be almost eliminated but also the conduction loss can be significantly reduced. The converter exhibits two distinct merits: first, there is no shoot-through issue because no active power switches are connected in series in each phase leg; second, the reverse recovery dissipation of the power switch is greatly reduced because there is no freewheeling current flowing through the body diode of power switches. The converter works as a rectifier when the power is transferred from ac grid to dc source. Alternately, it works as an inverter when the power is transferred from dc source to ac grid. The dissertation will show how this high-efficiency, high-reliability inverter can be used as the interface between the ac grid and the dc energy storage for bidirectional power flow operation [27]-[29]. It can also support reactive power flow and seamless energy transfer.

To better utilize the dc bus voltage and to eliminate the two dc bus capacitors, a novel bidirectional ac-dc converter is derived from Figure 1.5 by replacing the two-capacitor leg with a two-switch leg, as shown in Figure 1.6. The novel bidirectional ac-dc converter keeps the merits of the dual-buck converter based bidirectional ac-dc converter. Meanwhile the two large dc bus capacitors are eliminated.
To further reduce the size of the inductors, several novel topologies with optimized magnetic integration are also proposed.

### 1.3.3 Three-Phase Bidirectional AC-DC Converter

Three-phase ac-dc conversion of electric power is widely employed in motor drive, uninterruptible power supplies, and utility interfaces with renewable sources such as solar photovoltaic systems and battery energy storage systems. Numerous three-phase
topologies that have bidirectional flow capability have been reported [54]-[66]. The commonly used bidirectional converter topology consists of six power switches as shown in Figure 1.7. Without neutral connection, third harmonic will not exist. There is no need to eliminate 3rd, 9th, etc. triplen harmonics. Similar to the single-phase case, the power MOSFET cannot be used as the main switch in the three-phase converter since the intrinsic MOSFET body diode conduction could cause device failure. The IGBT can be used as the main switch for the three-phase converter, but their high switching and conduction losses normally limits to a lower switching frequency and larger filter size.

![Circuit diagram of a three-phase bidirectional ac-dc converter with split capacitors for neutral connection.](image)

Figure 1.8 Circuit diagram of a three-phase bidirectional ac-dc converter with split capacitors for neutral connection.

Three-phase converter with split capacitors for neutral connection is shown in Figure 1.8. Under unbalanced ac load condition, dc bus capacitors absorb the neutral current to maintain better balanced ac output. The problem with this topology is excessive current stress on split capacitors when ac loads or lines are highly unbalanced.

Three-phase four-leg converter is shown in Figure 1.9. Neutral leg is controlled to equalize the three-phase outputs. The features with this converter are less bulky capacitors and reduced size of passive components. However, control is more complicated.
A novel three-phase converter based on single-phase dual-buck converter is proposed, as shown in Figure 1.10. Besides the features of the single-phase dual-buck converter, the three-phase converter eliminates the two bulky dc bus capacitors.
1.3.4 Soft-Switching Techniques in Bidirectional AC-DC Converter

Soft-switching converters, especially zero-voltage switching (ZVS) inverters, on ac side using either coupled magnetic or split capacitors to reset resonant current have been studied for more than two decades [67]-[80]. Voltage source inverters also can achieve ZVS under rectifier mode. The auxiliary resonant commutated pole (ARCP) inverters achieve zero-voltage turn-on for main devices by using split capacitors to reset the resonant current [67]-[68]. However, the ARCP inverter needs extra control or circuits to balance the two dc link split capacitor voltages. In addition, the control for ZVS is complicated for the ARCP inverters.

As shown in Figure 1.11, the coupled magnetic type ZVS inverters have been proposed to avoid capacitor voltage balance issue [72]-[78]. These inverters all feature zero-voltage turn-on for main devices and zero-current turn-off for auxiliary devices. The control for ZVS is simple because of possible non-unity turns ratio for coupled magnetic [78]. However, the problem with these inverters is that the magnetizing current of the coupled magnetic cannot be reset [73]. A new soft-switching inverter using two small coupled magnetics in one resonant pole was proposed to solve magnetizing current

![Figure 1.11 Circuit diagram of a three-phase coupled magnetic type ZVS inverter.](image-url)
resetting problem [80]. A variable timing control scheme was also proposed to ensure the main devices operating at ZVS from zero to full load [79].

1.4 State-of-the-art Bidirectional AC-DC Converter Control

Current control is widely used in the grid-tie bidirectional ac-dc converter applications because the grid side voltage is controlled by the ac grid. Current control technologies can be divided into two groups: linear control such as proportional-integral (PI) control and proportional-resonant (PR) control; and non-linear control, such as sliding mode control and hysteresis control.

PI control is the most widely used control method for ac-dc converters. Although the PI control can provide fast dynamic response combined with other control schemes, it still has the steady-state error issue.

PR control can produce high gains at the desired frequencies to eliminate the steady-state error [81]. One problem with this scheme is the numerical accuracy in actual implementation.

Sliding mode control has been proposed in a variable structure control based power conditioning system. It provides fast dynamic response and robustness as a non-linear control scheme, but it is difficult to show numerical data of the stability by applying conventional feedback method.

Hysteresis control provides extremely fast response compared to other control methods. However, it is difficult to filter the high-frequency voltage and current components because the switching frequency is variable.

Various control schemes have been proposed for bidirectional ac-dc converter applications. However, most designs follow the unidirectional ac-dc converter or dc-ac inverter controller design methodology. No mode transition discussion has been addressed since the power management is normally not included in the system design. For the design without smooth mode transition consideration, it will cause large voltage and current stress on devices, which result in device failures.

In the dissertation, an admittance compensator along with a quasi-proportional-resonant controller (QPR) is adopted to allow smooth mode transition and elimination of the steady-state error over the entire load range [82]-[84].
1.5 Research Motivation

1.5.1 Battery SOC Estimation Challenge

SOC is used to determine battery capacity. Among all the practical techniques, Coulomb counting is the most popular method to estimate the battery SOC. However, this method is not very accurate since it does not consider the effects of the temperature and charging and discharging efficiency. On the other hand, there is no way to estimate the initial SOC, and the accuracy depends on sensor precision. Therefore, this dissertation adopts the Coulomb counting along with an accurate open circuit voltage model to estimate the SOC. The open circuit voltage is measured by a 14-bit ADC.

1.5.2 Charge Equalizer Design Challenge

Charge equalizer is used to balance the individual battery cells in a battery module. Among the active cell balancing schemes, bidirectional cell balancing offers the advantage of fast balancing time. However, it is difficult to implement bidirectional cell balancing in a lithium-ion battery string consisting of more than 100 cells in electric vehicle (EV) application. A modularized charge equalizer based on switched transformer and bidirectional converter dc-dc schemes is employed in this dissertation.

1.5.3 Bidirectional AC-DC Converter Topology

The high-efficiency MOSFET dual-buck converter is chosen as the bidirectional ac-dc converter. The major issue with this type of converter is the requirement of two separate inductors. However, without shoot-through concern and dead time requirement, the switching frequency can be pushed higher to reduce the size of the inductor while maintaining low ripple current content. The question is how to design the switching frequency and other parameters. In other words, the tradeoff between efficiency and cost needs to be optimized.

A novel bidirectional ac-dc converter is derived from the dual-buck based bidirectional ac-dc converter.
1.5.4 Bidirectional AC-DC Converter Mode Transition Control

One important design aspect of the system is the smooth power flow transition control of the bidirectional ac-dc converter. For the battery energy storage system, the control needs to manage the wide range current in and out of the batteries and meantime ensure all cell SOCs being strictly kept in boundaries for safety operation. The transition between rectifier mode and inverter mode needs to be fast and smooth enough to guarantee energy effectively transferred without causing system instability and failure.

A unified current controller is proposed to generate only one command instead of two separate commands for rectifier mode and inverter mode. The energy management can switch from one mode to the other mode immediately by changing the phase angle information of the current reference.

1.6 Research Outline

The research outline is list as follows.

- A dual-buck converter based bidirectional ac-dc converter is proposed. The dual-buck converter has not been used in rectifier mode operation. The implemented converter efficiency peaks at 97.8% at 50-kHz switching frequency for both rectifier and inverter modes.
- A novel bidirectional ac-dc MOSFET converter is proposed to eliminate the two dc bus capacitors. The implemented converter efficiency peaks at 98.0% at 50-kHz switching frequency for both rectifier and inverter modes.
- A unified digital controller is proposed to control the bidirectional power flow and stabilize the system in mode transition.
- With SOC balancing, the battery energy storage system has gained much more capacity than the system without SOC balancing.

The dissertation consists of six chapters, which are organized as follows.

Chapter 1 introduces the research background. The main research objective is to design a high-efficiency grid-tie battery energy storage system capable of smoothly transferring energy with grid. Various SOC estimation and charge equalization
approaches are described and discussed for the BMS. Different bidirectional ac-dc converter topologies are investigated. The dual-buck type converter is employed as the bidirectional ac-dc converter. Smooth mode transition in bidirectional power flow control is required in the system design. At last, the research objectives are proposed.

In Chapter 2, a high-efficiency bidirectional ac-dc converter adopts dual-buck converter architecture is proposed. A new SPWM scheme by using split SPWM as the main scheme and joint SPWM as the supplementary scheme for the zero-crossing region is proposed. The proposed bidirectional ac-dc converter consists of two buck converters under inverter mode, each operating during a half line cycle. As a result, the magnetic components are only utilized during the half line cycle. However, the utilization can be improved by integrating magnetic components such as transformers and inductors on the same core. Two different structures of magnetic integration are presented. One is employing one coupled inductor in series with small inductors, and the other is utilizing two coupled inductors in series. The implemented converter efficiency peaks at 97.8% at 50-kHz switching frequency for both rectifier and inverter modes.

In Chapter 3, to better utilize the dc bus voltage and eliminate the two dc bus capacitors, a novel bidirectional ac-dc converter is proposed by replacing the two-capacitor leg of the dual-buck converter based single-phase bidirectional ac-dc converter with a two-switch leg. The novel bidirectional ac-dc converter keeps the merits of the dual-buck converter based bidirectional ac-dc converter. Meanwhile the two large dc bus capacitors and related voltage-balancing control are eliminated. The novel bidirectional ac-dc converter consists of two boost converters under rectifier mode, each operating during a half line cycle. It consists of two buck converters under inverter mode, each operating during a half line cycle. As a result, the magnetic components are only utilized during the half line cycle. The low utilization of the magnetic components may be a serious penalty in terms of weight, power density, and cost. With magnetic integration, the total number of magnetic cores is reduced by half. Based on the single-phase bidirectional ac-dc converter topology, several novel three-phase bidirectional ac-dc converter topologies are proposed. Detailed operating principles are described.

In Chapter 4, in order to control the bidirectional power flow and at the same time stabilize the system in mode transition, a unified digital controller is proposed. The
differences between individual controllers and unified controller are described. The power stage small-signal model is derived for the dual-buck converter based single-phase bidirectional ac-dc converter. Based on the small-signal model, an admittance compensator along with a QPR controller is adopted to allow smooth startup and elimination of the steady-state error over the entire load range. The proposed QPR controller is designed and implemented with a digital controller. Then the coefficients of the digital controller are truncated into certain word length binary representation, so as to be fit to the numbers of bits available to the FPGA for variables and constants. The characteristics of the designed analog resonant controller, digital controller, and truncated digital controller are analyzed. The entire system has been simulated in both PSIM and Simulink and verified with hardware experiments. Both simulation and experimental results match well and validate the design of the proposed unified controller. Small transient currents are observed with the power transferred from rectifier mode to inverter mode at peak current point and also from inverter mode to rectifier mode at peak current point.

In Chapter 5, a high-efficiency grid-tie lithium-ion battery based energy storage system is presented. The system consists of three subsystems, a LiFePO₄ battery pack and associated BMS, a bidirectional ac-dc converter, and the central control unit which controls the operation mode and grid interface of the energy storage system. The designed BMS monitors and reports all battery cells parameters in the pack. Based on these parameters, the BMS controller estimates the SOC of each battery cell in the pack. The SOC information is then used to control the active cell balancing circuits to mitigate the mismatch among the series connected cells. The SOC and SOH information is also used by the central control unit to determine the operating mode of the energy storage system. Using the proposed SOC balancing technique, the entire battery storage system has demonstrated more capacity than the system without SOC balancing. Under the charging condition from 30% to 70% SOC and discharging condition from 70% to 30% SOC, the use of SOC balancing technique has 33% more capacity. The round-trip efficiency is 96.5% for the battery pack. The overall round-trip efficiency for the battery energy storage system consisting of battery pack with associated BMS and bidirectional ac-dc converter is 92.6%.
In Chapter 6, the conclusion is drawn, and future works are summarized based upon the implementation experience and experimental results.
Chapter 2  Dual-Buck Converter Based Bidirectional AC-DC Converter

2.1 Introduction

With the increased concerns on environment and cost of energy, renewable energy sources are emerging as attractive power supply sources because they are clean and renewable. In 2008, about 19% of global energy production came from renewables including with 13% traditional biomass and 3.2% hydroelectricity. New renewables such as small hydro, modern biomass, wind, solar, geothermal, and biofuels accounted for another 2.7% and are growing very rapidly [85]. California has mandated that 33% of its power come from renewables by 2020, which is shown in Table 2.1 [86].

<table>
<thead>
<tr>
<th></th>
<th>2007 (MW)</th>
<th>20% RPS 2012 (MW)</th>
<th>33% RPS 2020 (MW)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hydro (over 300 MW)</td>
<td>8,464</td>
<td>8,464</td>
<td>8,464</td>
</tr>
<tr>
<td>Nuclear</td>
<td>4,550</td>
<td>4,550</td>
<td>4,550</td>
</tr>
<tr>
<td>Fossil</td>
<td>27,205</td>
<td>29,100</td>
<td>33,000</td>
</tr>
<tr>
<td>Wind</td>
<td>2,688</td>
<td>7,723</td>
<td>12,826</td>
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<td>Solar</td>
<td>481</td>
<td>1,945</td>
<td>6,026</td>
</tr>
<tr>
<td>Geothermal</td>
<td>1,556</td>
<td>2,620</td>
<td>3,970</td>
</tr>
<tr>
<td>Hydro (up to 30 MW)</td>
<td>822</td>
<td>822</td>
<td>822</td>
</tr>
<tr>
<td>Biomass</td>
<td>787</td>
<td>1,008</td>
<td>1,778</td>
</tr>
<tr>
<td>Total Renewables</td>
<td>6,344</td>
<td>14,118</td>
<td>25,442</td>
</tr>
<tr>
<td>Total</td>
<td>45,653</td>
<td>56,232</td>
<td>71,436</td>
</tr>
</tbody>
</table>
Cumulative global photovoltaic (PV) installation surpassed 21 GW at the end of 2009 [87]. Wind power is growing at the rate of 30% annually, with a worldwide installed capacity of 158 GW in 2009 [87], and is widely used in Europe, Asia, and the United States.

The chart below (Figure 2.1) is from a California study on the irregular output of wind during 24 hours in Tehachapi [88]. It shows that the wind can drop off rapidly in the middle of the morning when the load is increasing as people arrive at work. Storage can save energy when the wind is blowing, and feed that energy back into the grid when the wind stops.

The renewable energy source based DG systems are normally interfaced to the grid through power electronic converters and energy storage systems. A systematic organization of these DG systems, energy storage systems, and a cluster of loads forms a microgrid, which is shown in Figure 2.2. Recent developments and advances in energy storage systems and power electronics technologies are making the application of energy storage technologies a viable solution for modern power applications [89]. Storage can be
sized in the kW range up to thousands of MW. Depending upon the utility requirements, energy storage such as battery or flywheel systems can be used to provide fast voltage and frequency regulation (second by second), load shifting (adjusting to shifts in wind and solar over timeframes of minutes to hours), volt-ampere reactive (VAR) support, and black start service. It can be designed for the needs of distribution or transmission. It can be designed for single purpose operation, or for multiple purposes. In order to meet the challenges of practical utility applications, an energy storage system should have ac-dc/dc-ac bidirectional power conversion capability, islanding function, and high round-loop efficiency.

![Energy storage systems based microgrid configuration.](image)

**Figure 2.2** Energy storage systems based microgrid configuration.

### 2.2 Motivation for High-Efficiency Bidirectional AC-DC Converter

The conventional power conversion between ac power and dc power can be classified into two categories: ac-dc conversion, which is known as rectifier mode or power factor
correction (PFC), and dc-ac conversion, which is known as inverter mode. Both conversions are widely used in unidirectional power flow applications.

In a battery energy storage system, a bidirectional ac-dc converter with a proper charging-discharging profile is required to transfer energy between the battery pack and the ac grid. The converter works as a rectifier when the power is transferred from ac grid to battery pack. Alternately, it works as an inverter when the power is transferred from battery pack to ac grid. To realize bidirectional power flow in ac-dc converters, the power switch should carry the current on both directions. It is usually implemented with the power MOSFET or the IGBT in parallel with a diode.

A traditional single-phase four-switch bidirectional ac-dc converter is shown in Figure 2.3. For this topology, the power MOSFET cannot be used as the main switch in the high-voltage high-power applications because the intrinsic MOSFET body diode reverse recovery could cause device failure.

Figure 2.4 shows the sub-operating modes under inverter mode for one switching cycle. When \( S_1 \) and \( S_4 \) are on, current \( i_L \) is increased because the voltage across inductor \( L \) is positive. When \( S_1 \) is off, Current \( i_L \) goes through \( S_4 \) and anti-parallelled diode of \( S_3 \). Current \( i_L \) is decreased because the voltage across inductor \( L \) is negative. In this case, if \( S_3 \) is replaced by a power MOSFET, the body diode of \( S_3 \) will conduct the current. Even if \( S_3 \) works under synchronous rectification when \( S_1 \) is off, the body diode of \( S_3 \) will
conduct the current during the dead time. Excessive reverse recovery current of the body diode will produce a tremendous amount of turn-on loss. Moreover, the loss could cause device failure.

Figure 2.4 Operating under inverter mode for one switching cycle. (a) $S_1$ and $S_4$ are on. (b) Diode of $S_3$ and $S_4$ are on.

Although the power MOSFET cannot be used as the main switch for the traditional single-phase four-switch bidirectional ac-dc converter, new semiconductor structure and process have made high-voltage power MOSFET much more efficient with exceptionally low on-state drain-to-source resistance ($R_{DS(on)}$). Extremely low switching and conduction losses make switching applications even more efficient, more compact, lighter and cooler.

The proposed high-efficiency bidirectional ac-dc converter in this chapter adopts opposed current half bridge inverter architecture [23]. Since it consists of two buck converters and also has features of the conventional half bridge inverter, it is named as dual-buck half bridge inverter [24]-[26]. The converter exhibits two distinct merits: first, there is no shoot-through issue because no active power switches are connected in series in each phase leg; second, the reverse recovery dissipation of the power switch is greatly reduced because there is no freewheeling current flowing through the body diode of power switches. It can also support reactive power flow and seamless energy transfer. For the control scheme, the admittance compensator along with a QPR controller is adopted to allow smooth startup and elimination of the steady-state error over the entire load range. The major issue with this type of converter is the requirement of two separate inductors. However, without shoot-through concern and dead time requirement, the
switching frequency can be pushed higher to reduce the size of the inductor while maintaining low ripple current content. Both simulation and experimental results match very well and validate the design features of the high-efficiency, high-reliability converter. The implemented converter efficiency peaks at 97.8% at 50-kHz switching frequency for both rectifier and inverter modes.

2.3 Proposed Single-Phase Bidirectional AC-DC Converter

2.3.1 Single-Phase Bidirectional AC-DC Converter Topology

![Circuit diagram of the proposed bidirectional ac-dc converter.](image)

Figure 2.5 shows the circuit diagram of the proposed dual-buck based bidirectional ac-dc converter [27]-[29]. The circuit consists of two power switches $a_1$ and $a_2$, two diodes $D_1$ and $D_2$, two inductors $L_1$ and $L_2$, and two split dc bus capacitors $C_1$ and $C_2$. The converter works as a rectifier when the power is transferred from ac grid to dc source. Alternately, it works as an inverter when the power is transferred from dc source to ac grid. The voltage across each capacitor $C_1$ and $C_2$ should be always larger than the peak ac voltage to ensure the circuit works properly throughout the whole line cycle.

In this converter, the leg consisting of $a_1$ and $D_1$ conducts positive current, and the leg consisting of $a_2$ and $D_2$ conducts negative current. Since $a_1$ and $a_2$ only conducts positive current, the power MOSFETs are used as main switches without body diode reverse recovery issue. The features with this converter are: (1) low conduction and turn-off loss
by using power MOSFETs, (2) less electromagnetic interference (EMI) without MOSFET body diode reverse recovery issue, (3) low turn-on loss by using ultrafast reverse recovery diodes, (4) no dead time and short-through concern, (5) bidirectional power flow and reactive power control capability.

2.3.2 Operating Principle

![Circuit Diagram](image)

**Figure 2.6** Definition of different modes based on phase angle difference between voltage and current waveforms. (a) Circuit diagram. (b) Inverter mode (In phase). (c) $i_{ac}$ lags $v_{ac}$ by 90°. (d) $i_{ac}$ leads $v_{ac}$ by 90°. (e) Rectifier mode (180° Out of phase).

The definition of different power transferring modes based on phase angle difference between voltage and current waveforms are shown in Figure 2.6. For pure active power transferring, there are two modes: inverter mode in which voltage and current are in phase and rectifier mode in which voltage and current are 180° out of phase. For reactive
power transferring, the phase angle differences between voltage and current are neither $0^\circ$ nor $180^\circ$. Two examples with pure reactive power transferring are shown in Figure 2.6(c) in which $i_{ac}$ lags $v_{ac}$ by $90^\circ$ and Figure 2.6(d) in which $i_{ac}$ leads $v_{ac}$ by $90^\circ$.

![Diagram of power transferring](image)

**Figure 2.7** Operating under rectifier mode with pure active power transferring. (a) Conceptual voltage and current waveform. (b) $a_1$ is on. (c) $D_1$ is on. (d) $a_2$ is on. (e) $D_2$ is on.

Figure 2.7 and Figure 2.8 show the four sub-operating modes under rectifier and inverter modes, respectively. For the rectifier mode with pure active power transferring, there are four sub-operating modes depending on the conducting status of $a_1$, $a_2$, $D_1$ and $D_2$.

In the positive half cycle, leg $a_1$ and $D_1$ operates. When $a_1$ is on, current $i_{ac}$ is increased because the voltage across inductor $L_1$ is positive,
\[ V_{L1} = L_1 \frac{di_{ac}}{dt} = V_{c1} + v_{ac} > 0. \] (2.1)

Capacitor \( C_1 \) is discharged, and the energy of both \( C_1 \) and \( C_2 \) is transferred to the dc sources. When \( a_1 \) is off and \( D_1 \) is on, current \( i_{ac} \) is decreased because the voltage across inductor \( L_1 \) is negative,

\[ V_{L1} = L_1 \frac{di_{ac}}{dt} = -V_{c2} + v_{ac} < 0. \] (2.2)

Capacitor \( C_2 \) is charged, and the energy of both \( C_1 \) and \( C_2 \) is transferred to the dc sources.

In the negative half cycle, leg \( a_2 \) and \( D_2 \) operates. When \( a_2 \) is on, current \( i_{ac} \) is increased because the voltage across inductor \( L_2 \) is positive,

\[ V_{L2} = L_2 \frac{di_{ac}}{dt} = V_{c2} + v_{ac} > 0. \] (2.3)

Capacitor \( C_2 \) is discharged, and the energy of both \( C_1 \) and \( C_2 \) is transferred to the dc sources. When \( a_2 \) is off and \( D_2 \) is on, current \( i_{ac} \) is decreased because the voltage across the inductor \( L_2 \) is negative,

\[ V_{L2} = L_2 \frac{di_{ac}}{dt} = -V_{c1} + v_{ac} < 0. \] (2.4)

Capacitor \( C_1 \) is charged, and the energy of both \( C_1 \) and \( C_2 \) is transferred to the dc sources.

Overall, in the positive half cycle \( C_1 \) is always discharged, but \( C_2 \) is always charged. However, in the negative half cycle \( C_1 \) is always charged, but \( C_2 \) is always discharged. The charge balance is maintained through the entire line cycle.

For the inverter mode pure active power transferring, all the analysis is similar to that of rectifier mode except that the current and voltage are in phase; therefore, the energy is transferred from dc sources to ac grid. Based on the above analysis, it can be concluded
that $C_2$ is always charged in the positive half cycle and $C_1$ is always charged in the negative half cycle, and the charge balance maintains through the entire line cycle.

![Diagram](image)

Figure 2.8 Operating under inverter mode with pure active power transferring. (a) Conceptual voltage and current waveform. (b) $a_1$ is on. (c) $D_1$ is on. (d) $a_2$ is on. (e) $D_2$ is on.

To transfer reactive power between ac grid and dc sources, the operation of the circuit becomes much more complicated. Based on the direction of the ac current and voltage, one ac line cycle can be divided into 4 regions, which is shown in Figure 2.9. Only the leg that conducts current is shown here for simplicity. In region 1, current is negative and voltage is positive. Leg $a_2$ and $D_2$ conducts the current. In region 2, both current and voltage are positive. Leg $a_1$ and $D_1$ conducts the current. Region 3 is similar to region 2 except that voltage is negative. Region 4 is similar to region 1 except that voltage is negative. Based on above analysis, it can be concluded that the leg consisting of $a_1$ and
$D_1$ conducts positive current, and the leg consisting of $a_2$ and $D_2$ conducts negative current whenever voltage is positive or negative.

![Diagram](image)

Figure 2.9 Operating under active and reactive power transferred between ac grid and dc source. (a) Conceptual voltage and current waveform. (b) Region 1, $a_2$ and $D_2$ are on. (c) Region 2, $a_1$ and $D_1$ are on. (d) Region 3, $a_1$ and $D_1$ are on. (e) Region 4, $a_2$ and $D_2$ are on.

2.3.3 Inductor Design and Optimization

Inductor design has significant impact on system performance, such as the device switching loss, inductor loss, and system volume etc. It is necessary to design and optimize the inductance with all design considerations.

Take Figure 2.8 (b) and (c) as one switching cycle to calculate the inductance. Assume the input power is 1 kW and the ac rms voltage is 30 V, the ac rms current can be calculated as
\[ I_{\text{ac rms}} = \frac{P_{\text{ac}}}{v_{\text{ac rms}}} = \frac{1000}{30} = 33 \text{ A} . \]  

(2.5)

Ripple current needs to be minimized. 5% peak-to-peak inductor ripple current is used as the design target. The switching frequency of the ac-dc converter is designed as 50 kHz. The inductance can be calculated as

\[ L = \frac{\Delta V}{\Delta i} \Delta t = \frac{V_{\text{ac}} / 2 - v_{\text{ac}}}{5\% \cdot I_{pk}} \cdot d_{a1 \_ inv} T_s . \]  

(2.6)

From Figure 2.8(b) and (c), when current is positive in the inverter mode, the total volt-seconds applied to the inductor \( L_1 \) over one switching period are as follows:

\[ \left( \frac{V_{\text{dc}}}{2} - v_{\text{ac}} \right) \cdot d_{a1 \_ inv} + \left( -\frac{V_{\text{dc}}}{2} - v_{\text{ac}} \right) \cdot (1 - d_{a1 \_ inv}) = 0 . \]  

(2.7)

The duty cycle for switch \( a_1 \) can be derived as

\[ d_{a1 \_ inv} = \frac{1}{2} \left( 1 + \frac{v_{\text{ac}}}{V_{\text{dc}} / 2} \right) = \frac{1}{2} \left( 1 + \frac{v_{pk} \sin \omega t}{V_{\text{dc}} / 2} \right) = 0.5 \cdot (1 + M \sin \omega t) \]  

(2.8)

where \( M = \frac{v_{pk}}{V_{\text{dc}}/2} \) is modulation index and \( \sin \omega t > 0 \).

Then the inductance can be calculated as

\[ L = \frac{\Delta V}{\Delta i} \Delta t = \frac{V_{\text{ac}} / 2 - v_{\text{ac}}}{5\% \cdot I_{pk}} \cdot d_{a1 \_ inv} T_s = \frac{0.25 \cdot V_{\text{dc}} \cdot (1 - M \sin \omega t) \cdot (1 + M \sin \omega t) \cdot T_s}{5\% \cdot I_{pk}} \leq \frac{0.25 \cdot V_{\text{dc}} \cdot T_s}{5\% \cdot I_{pk}} = \frac{0.25 \cdot 120 \cdot 1}{5\% \cdot \sqrt{2} \cdot 33 \cdot 50000} = 257 \mu\text{H} . \]  

(2.9)
Inductor core materials influence the core power loss a lot for the same ripple current. Typical magnetic materials are silicon iron, amorphous, Finemet, ferrite and powder. Silicon iron is not considered because it is very lossy with high frequency components. Amorphous and Finemet are acceptable with loss, but they need air gap to avoid saturation. Audible noise will be a major problem with such materials. Ferrite is good for high frequency, but with high $\mu$, it also needs air gap. Audible noise again is a problem. Powder cores are good choice for PFC circuits as well as inverter filter applications because their higher saturation flux density provides a higher energy storage capability than can be obtained with gapped ferrites of the same size and effective permeability. High saturation flux density can also avoid core saturation during transient or startup when a large transient current spike is likely to occur. Another advantage is it helps reduce the air gap and the related gap loss.

Among the three powder materials, molypermalloy powder, high flux and Kool $M\mu$, Kool $M\mu$ is preferred for its low core loss and low relative cost. The high flux density and low core losses make Kool $M\mu$ cores excellent for use in PFC circuits as well as inverter applications.

Table 2.2 Comparison of design results based on different Kool $M\mu$ cores

<table>
<thead>
<tr>
<th></th>
<th>77191</th>
<th>77192</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mu$</td>
<td>26</td>
<td>60</td>
</tr>
<tr>
<td>$A_L$ (nH/turn^2)</td>
<td>60</td>
<td>138</td>
</tr>
<tr>
<td>$N$ (turn)</td>
<td>27 (6 cores)</td>
<td>25 (3 cores)</td>
</tr>
<tr>
<td>$H_{pk}$ (Oer)</td>
<td>128.57</td>
<td>119</td>
</tr>
<tr>
<td>$B_{pk}$ (G)</td>
<td>3.14</td>
<td>5.59</td>
</tr>
<tr>
<td>Core Loss (W)</td>
<td>3.1</td>
<td>1.57</td>
</tr>
<tr>
<td>Copper Loss (W)</td>
<td>18.38</td>
<td>10.16</td>
</tr>
<tr>
<td>Total Loss (W)</td>
<td>21.48</td>
<td>11.73</td>
</tr>
</tbody>
</table>
Table 2.2 is the comparison of design results based on different Kool Mμ cores. The results show that the copper losses dominate the total losses in this case. The 77192 core is preferred since it generates lower losses than the 77191 core.

Overall, lower-μ type Kool Mμ is preferred for high-power filter applications. However, a tradeoff between core and copper losses should be determined to help overall loss reduction.

2.3.4 Zero-Crossing Distortion and Solution

Sinusoidal pulse width modulation (SPWM) method is a popular linear modulation scheme for rectifiers and inverters. A split SPWM scheme is proposed in this paper.

![Figure 2.10 Waveforms of ac voltage, ac current and inductor currents under split SPWM.](image)

The basic principle of split SPWM is that leg \( a_1 \) & \( D_1 \) and leg \( a_2 \) & \( D_2 \) operate alternatively in one line cycle according to the direction of the ac current \( i_{ac} \). Leg \( a_1 \) & \( D_1 \) conducts positive half-cycle current while leg \( a_2 \) & \( D_2 \) conducts negative half-cycle
current. The key waveform of ac voltage, ac current and inductor currents are offered in Figure 2.10. The definition of ac current $i_{ac}$ is defined as

$$i_{ac} = \begin{cases} i_{L1} & i_{ac} > 0 \\ -i_{L2} & i_{ac} \leq 0 \end{cases}$$  \hspace{1cm} (2.10)$$

Figure 2.11 shows the equivalent circuit of the converter under split SPWM. In this circuit, $v_{L1}$ and $v_{L2}$ are equivalent square waveform voltage sources.

![Equivalent circuit of the converter under split SPWM.](image)

Figure 2.12  Current waveform of DCM near zero-crossing region under split SPWM.
Since only one device is conducting at any given time, conduction and switching losses are relatively low. However, when the inductor currents are small enough, the converter enters discontinuous conduction mode (DCM) as shown in Figure 2.12. The characteristic of the converter changes significantly in DCM and the regulation of ac current requires quick system response.

![Current waveforms under joint SPWM.](image)

Figure 2.13 Current waveforms under joint SPWM.

To solve the current zero-crossing distortion problem, another SPWM named joint SPWM is proposed.

The basic principle of joint SPWM is that both leg $a_1 \& D_1$ and leg $a_2 \& D_2$ operate at the same time. The positive current goes through leg $a_1 \& D_1$ while the negative current goes through leg $a_2 \& D_2$. The sum of the two currents forms the ac sinusoidal current. The current waveforms are shown in Figure 2.13. The definition of ac current $i_{ac}$ is expressed as

$$i_{ac} = i_{L1} + i_{L2} \tag{2.11}$$

Figure 2.14 shows the equivalent circuit of the converter under joint SPWM. In this circuit, $v_{L1}$ and $v_{L2}$ are equivalent square waveform voltage sources, which swing between $-V_{dc}/2$ and $+V_{dc}/2$.

When the inductor currents are small, the converter is still operating in continuous conduction mode (CCM) as shown in Figure 2.15. Compared with the converter
operating under split SPWM, the switching and conduction losses are doubled under joint SPWM since two devices are conducting at the same time.

![Equivalent circuit of the converter under joint SPWM.](image)

**Figure 2.14** Equivalent circuit of the converter under joint SPWM.

![Current waveform near zero-crossing region under joint SPWM.](image)

**Figure 2.15** Current waveform near zero-crossing region under joint SPWM.

To obtain the advantages of both SPWM schemes, a new SPWM scheme by using split SPWM as the main scheme and joint SPWM as the supplementary scheme for the zero-crossing region is proposed. On one hand, since split SPWM is utilized as the main scheme, conduction and switching losses are relatively low. On the other hand, because joint SPWM is employed for the zero-crossing region, the ac current zero-crossing distortion problem is solved.
Figure 2.16  Simulation results of the converter under split SPMW. (a) Waveforms over cycles. (b) Waveforms near zero-crossing region

Figure 2.16 shows the simulation results of the converter under split SPWM. Figure 2.16(a) shows the waveforms over cycles. Figure 2.16(b) shows the waveforms near zero-crossing region.
Figure 2.17 Simulation results of the converter under joint SPWM. (a) Waveforms over cycles. (b) Waveforms near zero-crossing region.

Figure 2.17 shows the simulation results of the converter under joint SPWM. Figure 2.17(a) shows the waveforms over cycles. Figure 2.17(b) shows the waveforms near zero-crossing region.
Figure 2.18 Simulation results of the converter under the proposed new SPWM. (a) Waveforms over cycles. (b) Waveforms near zero-crossing region.

Figure 2.18 shows the simulation results of the converter under the proposed new SPWM. Figure 2.18(a) shows the waveforms over cycles. Figure 2.18(b) shows the waveforms near zero-crossing region.
Figure 2.19 Experimental results of the converter. (a) Results under split SPWM. (b) Results under the proposed new SPWM.

Figure 2.19(a) and (b) show the experimental results of the converter under split SPWM and the proposed new SPWM, respectively. As can be seen in Figure 2.19(b), the proposed new SPWM effectively solves the ac current zero-crossing distortion problem.
2.3.5 Simulation Results

Figure 2.20 Simulation results under (a) rectifier mode and (b) inverter mode, both with $v_{ac} = 30 \text{ V}_{\text{rms}}$ and $i_{ac} = 23 \text{ A}_{\text{rms}}$.

Figure 2.20(a) and (b) shows the simulation results under both rectifier and inverter modes for the converter, respectively.
Figure 2.21 Simulation results with reactive power flow. (a) Current leads voltage by 90°. (b) Current lags voltage by 90°.

Figure 2.21(a) and (b) show simulated waveforms of reactive power flow. Figure 2.21(a) shows current leads voltage by 90°. Figure 2.21(b) shows current lags voltage by 90°.
2.3.6 Experimental Results

Figure 2.22 Experimental results under (a) rectifier mode and (b) inverter mode, both with $v_{ac} = 30 \, V_{rms}$ and $i_{ac} = 23 \, A_{rms}$.

Figure 2.22(a) and (b) shows the experimental results under both rectifier and inverter modes for the converter, respectively.
Figure 2.23 Experimental results with reactive power flow. (a) Current leads voltage by 90°. (b) Current lags voltage by 90°.

Figure 2.23(a) and (b) show experimental waveforms of reactive power flow. Figure 2.23(a) shows current leads voltage by 90°. Figure 2.23(b) shows current lags voltage by 90°.
The bidirectional power flow capability of the proposed circuit is well verified. Figure 2.24 shows the photograph of the bidirectional ac-dc converter prototype. The field-programmable gate array (FPGA) board that implements the controller function is separated from the main power board. Figure 2.25 shows the experimental efficiency of the proposed converter under both rectifier and inverter modes. The efficiency peaks at 97.8% at 50-kHz switching frequency for both rectifier and inverter modes.

![Figure 2.24 Prototype of the proposed bidirectional ac-dc converter.](image)

**Figure 2.24** Prototype of the proposed bidirectional ac-dc converter.

![Figure 2.25 Experimental efficiency for both rectifier and inverter modes.](image)

**Figure 2.25** Experimental efficiency for both rectifier and inverter modes.
2.4 Single-Phase Bidirectional AC-DC Converter with Magnetic Integration

![Diagram](image)

Figure 2.26 The proposed converter operating under inverter mode during the period when ac current is positive.

![Diagram](image)

Figure 2.27 The proposed converter operating under inverter mode during the period when ac current is negative.

The proposed single-phase bidirectional ac-dc converter in Figure 2.5 consists of two buck converters under inverter mode. One buck converter operates while the other buck converter is inoperative, as indicated in Figure 2.26 and Figure 2.27. Each converter operates in a half line cycle. Accordingly, the magnetic components, $L_1$ and $L_2$, are only utilized in a half line cycle. The low utilization of the magnetic components may impose a serious penalty on system cost and power density.

However, the utilization can be improved by integrating the magnetic components. The utilization of the magnetic components in Figure 2.5 can be significantly improved by employing different coupled inductor structures. Two different structures of magnetic...
integration are presented. One is to employ one coupled inductor in series with small inductors and the other one is to utilize two coupled inductors in series.

2.4.1 Coupled Inductor in Series with Small Inductors

The circuit diagram of the implementation with one coupled inductor is shown in Figure 2.28. In the circuit, two small inductors $L_a$ and $L_b$ are employed to block the undesired circulating current due to the imbalance of the inductance of the coupled inductor.

![Figure 2.28 Bidirectional ac-dc converter with one coupled inductor.](image)

As shown in Figure 2.29, during the period when ac current is positive (no matter ac voltage is positive or negative), the circuit consists of switch $a_1$, diode $D_1$, inductor $L_a$ and winding $N_A$ operates to conduct the current, while the circuit consists of switch $a_2$, diode $D_2$, inductor $L_b$ and winding $N_B$ is idle. Similarly, as shown in Figure 2.30, during the period when ac current is negative (no matter ac voltage is positive or negative), the circuit consists of switch $a_2$, diode $D_2$, inductor $L_b$ and winding $N_B$ operates to conduct the current, while the circuit consists of switch $a_1$, diode $D_1$, inductor $L_a$ and winding $N_A$ is idle.
Figure 2.29 The proposed converter operating during the period when ac current is positive. The inactive components are shown in dashed lines.

Figure 2.30 The proposed converter operating during the period when ac current is negative. The inactive components are shown in dashed lines.
In order to analyze the effects of magnetizing and leakage inductance of the coupled inductor on the operation of the bidirectional ac-dc converter under inverter mode in Figure 2.28, the coupled inductor with a unity turns ratio is represented with a symmetrical model, as shown in Figure 2.31 [90]. In the symmetrical model, each side of the coupled inductor is represented with a magnetizing inductance connected in parallel with the corresponding winding and with a leakage inductance connected in series with the corresponding winding. The value of the magnetizing inductance connected in parallel with each winding of the ideal transformer is twice the total magnetizing inductance of the inductor, $L_{ma} = L_{mb} = 2L_m$.

With voltage and current reference directions under inverter mode as in Figure 2.31, the following voltage relationships can be easily established:

$$v_{a1} = v_{b1}$$  
$$v_{a1} = 2L_m \frac{di_{ma}}{dt}$$  
$$v_{b1} = 2L_m \frac{di_{mb}}{dt}.$$

From (2.12), (2.13) and (2.14), one can obtain
\[ i_{ma} = i_{mb} = i_m. \quad (2.15) \]

Similarly, from Figure 2.31, the following current relationship can be written:

\[ i_{a1} = -i_{b1} = i_T \quad (2.16) \]
\[ i_a = i_{ma} + i_{a1} \quad (2.17) \]
\[ i_b = i_{mb} + i_{b1}. \quad (2.18) \]

By using (2.15) and (2.16), current \( i_a \) and \( i_b \) can be expressed as:

\[ i_a = i_m + i_T \quad (2.19) \]
\[ i_b = i_m - i_T. \quad (2.20) \]

When leg \( a_1 \) and \( D_1 \) is operating and leg \( a_2 \) and \( D_2 \) is idle, one can get \( i_b = 0 \) and \( i_m = i_T \).

Apply Kirchhoff’s Voltage Law (KVL) when \( a_1 \) is on and \( D_1 \) is off as shown in Figure 2.32, the following voltage relationship can be obtained

\[ \frac{V_{dc}}{2} = (L_a + L_{tha}) \frac{di_a}{dt} + 2L_m \frac{di_{ma}}{dt} + v_{ac}. \quad (2.21) \]

Figure 2.32  The proposed converter with one coupled inductor operating under inverter mode when ac current is positive and \( a_1 \) is on.
By using (2.15), (2.19) and (2.21), voltage $v_{a1}$ can be expressed as

$$v_{a1} = L_m \frac{di_a}{dt} = \left( \frac{V_{dc}}{2} - v_{ac} \right) \frac{L_m}{(L_a + L_{ka}) + L_m}.$$  \hspace{1cm} (2.22)

By using (2.12), the voltage of point B relative to neutral point N can be expressed as

$$-\frac{V_{dc}}{2} < V_{bN} = \left( \frac{V_{dc}}{2} - v_{ac} \right) \frac{L_m}{(L_a + L_{ka}) + L_m} + v_{ac} < \frac{V_{dc}}{2}.$$  \hspace{1cm} (2.23)

Obviously, $a_2$ and $D_2$ will never be forced on.

Apply KVL when $a_1$ is off and $D_1$ is on as shown in Figure 2.33, the following voltage relationship can be obtained

$$-\frac{V_{dc}}{2} = (L_a + L_{ka}) \frac{di_a}{dt} + 2L_m \frac{di_{ma}}{dt} + v_{ac}.$$  \hspace{1cm} (2.24)

By using (2.15), (2.19) and (2.24), voltage $v_{a1}$ can be expressed as
\[ v_{a1} = L_m \frac{di_a}{dt} = \left( -\frac{V_{dc}}{2} - v_{ac} \right) \frac{L_m}{(L_a + L_{th}) + L_m}. \] (2.25)

By using (2.12), the voltage of point B relative to neutral point N can be expressed as

\[ -\frac{V_{dc}}{2} < V_{BN} = \left( -\frac{V_{dc}}{2} - v_{ac} \right) \frac{L_m}{(L_a + L_{th}) + L_m} + v_{ac} < \frac{V_{dc}}{2}. \] (2.26)

Again, \( a_2 \) and \( D_2 \) will never be forced on.

When leg \( a_2 \) and \( D_2 \) is operating and leg \( a_1 \) and \( D_1 \) is idle, one can get \( i_a = 0 \). When \( a_2 \) is on and \( D_2 \) is off, the voltage of point A relative to neutral N can be expressed as

\[ -\frac{V_{dc}}{2} < V_{AN} = \left( -\frac{V_{dc}}{2} - v_{ac} \right) \frac{L_m}{(L_b + L_{th}) + L_m} - v_{ac} < 0. \] (2.27)

Apparently, \( a_1 \) and \( D_1 \) will never be forced on.

When \( a_2 \) is off and \( D_2 \) is on, the voltage of point A relative to neutral N can be expressed as

\[ 0 < V_{AN} = \left( \frac{V_{dc}}{2} + v_{ac} \right) \frac{L_m}{(L_b + L_{th}) + L_m} - v_{ac} < \frac{V_{dc}}{2}. \] (2.28)

Similarly, \( a_1 \) and \( D_1 \) will never be forced on.

Same conclusions can be drawn for the converter operating under rectifier mode.

Figure 2.34(a) and (b) shows the simulation results under both rectifier and inverter modes for the converter, respectively. It can be concluded that one leg operates while the other leg is idle.
Figure 2.34 Simulation results of the proposed converter with one coupled inductor under (a) rectifier mode and (b) inverter mode.
Figure 2.35  Experimental results of the proposed converter with one coupled inductor under (a) rectifier mode and (b) inverter mode.

Figure 2.35(a) and (b) shows the experimental results under both rectifier and inverter modes for the converter, respectively.
2.4.2 Two Coupled Inductors in Series

![Diagram of Bidirectional AC-DC Converter with Two Coupled Inductors](image)

Figure 2.36 Bidirectional ac-dc converter with two coupled inductors.

The other method of magnetic integration is shown in Figure 2.36. Although there are still two coupled inductors in the circuit, the size and weight of the inductors are greatly reduced.

![Graph of AC Current vs Time](image)

Figure 2.37 The proposed converter operating during the period when ac current is positive. The inactive components are shown in dashed lines.
Figure 2.38 The proposed converter operating during the period when ac current is negative. The inactive components are shown in dashed lines.

As shown in Figure 2.37, during the period when ac current is positive (no matter ac voltage is positive or negative), the circuit consists of switch $a_1$, diode $D_1$, and windings $N_{A1}$ and $N_{A2}$ operate to conduct the current, while the circuit consists of switch $a_2$, diode $D_2$, and windings $N_{B1}$ and $N_{B2}$ is idle. Similarly, as shown in Figure 2.38, during the period when ac current is negative (no matter ac voltage is positive or negative), the circuit consists of switch $a_2$, diode $D_2$, and windings $N_{B1}$ and $N_{B2}$ operates to conduct the current, while the circuit consists of switch $a_1$, diode $D_1$, and windings $N_{A1}$ and $N_{A2}$ is idle. With magnetic integration, the power density is significantly improved and the weight of the converter is reduced.

In order to analyze the effects of magnetizing and leakage inductance of the coupled inductor on the operation of the bidirectional ac-dc converter under rectifier mode in Figure 2.36, the coupled inductor with a unity turns ratio is represented with a symmetrical model, as shown in Figure 2.39 [90]. In the symmetrical model, each side of the coupled inductor is represented with a magnetizing inductance connected in parallel with the corresponding winding and with a leakage inductance connected in series with the corresponding winding. The value of the magnetizing inductance connected in
parallel with each winding of the ideal transformer is twice the total magnetizing inductance of the inductor.

![Symmetrical model of the proposed converter with two coupled inductors under rectifier mode.](image)

**Figure 2.39** Symmetrical model of the proposed converter with two coupled inductors under rectifier mode.

With voltage and current reference directions under rectifier mode as in Figure 2.39, the following voltage relationships can be easily established:

\[
v_{a_1} = -v_{b_1} \quad (2.29)
\]
\[
v_{a_2} = v_{b_2} \quad (2.30)
\]
\[
v_{a_1} = 2L_{m1} \frac{di_{ma1}}{dt} \quad (2.31)
\]
\[
v_{b_1} = 2L_{m1} \frac{di_{mb1}}{dt} \quad (2.32)
\]
\[
v_{a_2} = 2L_{m2} \frac{di_{ma2}}{dt} \quad (2.33)
\]
\[
v_{b_2} = 2L_{m2} \frac{di_{mb2}}{dt} \quad (2.34)
\]

From (2.29), (2.31) and (2.32), one can obtain

\[
i_{ma1} = -i_{mb1} = i_{m1} \quad (2.35)
\]
whereas from (2.30), (2.33) and (2.34)

\[ i_{m2} = i_{mb/2} = i_{m2}. \]  \hspace{1cm} (2.36)

Similarly, from Figure 2.39, the following current relationship can be written:

\[ i_{a1} = i_{p1} \]  \hspace{1cm} (2.37)

\[ i_{a2} = -i_{b2} \]  \hspace{1cm} (2.38)

\[ i_a = i_{ma1} + i_{a1} = i_{ma2} + i_{a2} \]  \hspace{1cm} (2.39)

\[ i_b = i_{mb1} + i_{b1} = i_{mb2} + i_{b2}. \]  \hspace{1cm} (2.40)

Using (2.35) – (2.38) and adding (2.39) and (2.40), it follows that

\[ i_{a1} = i_{b1} = i_{m2}. \]  \hspace{1cm} (2.41)

\[ i_{a2} = -i_{b2} = i_{m1}. \]  \hspace{1cm} (2.42)

Also, by using (2.35) and (2.41), current \( i_a \) can be obtained as

\[ i_a = i_{m1} + i_{m2}. \]  \hspace{1cm} (2.43)

whereas by using (2.35) and (2.41), current \( i_b \) can be obtained as

\[ i_b = -i_{m1} + i_{m2}. \]  \hspace{1cm} (2.44)

During the positive ac current half cycle, leg \( a_1 \) and \( D_1 \) is operating and leg \( a_2 \) and \( D_2 \) is idle. When \( a_1 \) is on and \( D_1 \) is off as shown in Figure 2.40, on can get
\[ v_{h1} + v_{h2} + \left(L_{ab1} + L_{ab2}\right) \frac{di_b}{dt} = 0. \] (2.45)

The same result (2.45) also can be obtained when \(a_1\) is off and \(D_1\) is on as shown in Figure 2.41.

Similarly, during the negative ac current half cycle, when leg \(a_2\) and \(D_2\) is operating and leg \(a_1\) and \(D_1\) is idle, one can get
\[ v_{a1} + v_{a2} + (L_{lkb1} + L_{lkb2}) \frac{di_a}{dt} = 0. \] (2.46)

Using (2.32), (2.34), (2.35), (2.36), (2.44) and (2.45), the relationship between \( i_{m1} \) and \( i_{m2} \) during the positive ac current half cycle can be expressed as

\[ i_{m1} = \frac{L_{m2} + (L_{lkb1} + L_{lkb2})/2}{L_{m1} + (L_{lkb1} + L_{lkb2})/2} i_{m2}. \] (2.47)

Substituting (2.47) into (2.43) yields

\[ i_a = i_{m1} + i_{m2} = \frac{L_{m1} + L_{m2} + (L_{lkb1} + L_{lkb2})/2}{L_{m1} + (L_{lkb1} + L_{lkb2})/2} i_{m2}. \] (2.48)

whereas substituting (2.47) into (2.44) yields

\[ i_b = -i_{m1} + i_{m2} = \frac{L_{m1} - L_{m2}}{L_{m1} + (L_{lkb1} + L_{lkb2})/2} i_{m2}. \] (2.49)

Eliminating \( i_{m2} \) from (2.48) and (2.49), the relationship between \( i_a \) and \( i_b \) can be derived as

\[ \frac{i_b}{i_a} = \frac{L_{m1} - L_{m2}}{L_{m1} + L_{m2} + (L_{lkb1} + L_{lkb2})}. \] (2.50)

As can be seen from (2.50), for \( L_{m1} = L_{m2} \), no ripple current is returned through windings \( N_{B1} \) and \( N_{B2} \) regardless of their leakage inductance. If \( L_{m1} \neq L_{m2} \), the amount of the ripple current returned through windings \( N_{B1} \) and \( N_{B2} \) is determined by the difference between the two magnetizing inductances.

Similarly, during the negative ac current half cycle, when leg \( a_2 \) and \( D_2 \) is operating and leg \( a_1 \) and \( D_1 \) is idle, the relationship between \( i_a \) and \( i_b \) can be derived as
\[
\frac{i_a}{i_b} = \frac{L_{m1} - L_{m2}}{L_{m1} + L_{m2} + (L_{\text{m1}} + L_{\text{m2}})}.
\] (2.51)

Due to symmetrical operation, the behavior of the circuit during the negative ac current half cycle is identical to that during the positive ac current half cycle. If \(L_{m1} \neq L_{m2}\), the amount of the ripple current returned through windings \(N_{A1}\) and \(N_{A2}\) is determined by the difference between the two magnetizing inductances.

Under inverter mode during the positive ac current half cycle, when leg \(a_1\) and \(D_1\) is operating and leg \(a_2\) and \(D_2\) is idle, the relationship between \(i_a\) and \(i_b\) can be derived as

\[
\frac{i_b}{i_a} = \frac{L_{m1} - L_{m2}}{L_{m1} + L_{m2} + (L_{\text{m1}} + L_{\text{m2}})}.
\] (2.52)

If \(L_{m1} \neq L_{m2}\), the amount of the ripple current returned through windings \(N_{B1}\) and \(N_{B2}\) is determined by the difference between the two magnetizing inductances.

Under inverter mode during the negative ac current half cycle, when leg \(a_2\) and \(D_2\) is operating and leg \(a_1\) and \(D_1\) is idle, the relationship between \(i_a\) and \(i_b\) can be derived as

\[
\frac{i_a}{i_b} = \frac{L_{m1} - L_{m2}}{L_{m1} + L_{m2} + (L_{\text{m1}} + L_{\text{m2}})}.
\] (2.53)

Due to symmetrical operation, the behavior of the circuit during the negative ac current half cycle is identical to that during the positive ac current half cycle.

Figure 2.42(a) and (b) shows the simulation results under both rectifier and inverter modes for the converter, respectively. It can be concluded that one leg operates while the other leg is idle.
Figure 2.42 Simulation results of the proposed converter with two coupled inductors under 
(a) rectifier mode and (b) inverter mode.
Figure 2.43 Experimental results of the proposed converter with two coupled inductors under (a) rectifier mode and (b) inverter mode.
Figure 2.43(a) and (b) shows the experimental results under both rectifier and inverter modes for the converter, respectively. The efficiency of the converter with two coupled inductors is the same as the converter without magnetic integration.

2.5 Summary

The renewable energy source based DG systems are normally interfaced to the grid through power electronic converters and energy storage systems. Recent developments and advantages in energy storage and power electronics technologies are making the application of energy storage technologies a viable solution for modern power applications. In order to meet the challenges of practical utility applications, an energy storage system should have ac-dc/dc-ac bidirectional power conversion capability, islanding function, and high round-loop efficiency.

The proposed high-efficiency bidirectional ac-dc converter in this chapter adopts opposed current half bridge inverter architecture. Since it consists of two buck converters and also has features of the conventional half bridge inverter, it is named as dual-buck half bridge inverter. The converter exhibits two distinct merits: first, there is no shoot-through issue because no active power switches are connected in series in each phase leg; second, the reverse recovery dissipation of the power switch is greatly reduced because there is no freewheeling current flowing through the body diode of power switches. The implemented converter efficiency peaks at 97.8% at 50-kHz switching frequency for both rectifier and inverter modes.

A new SPWM scheme by using split SPWM as the main scheme and joint SPWM as the supplementary scheme for the zero-crossing region is proposed. On one hand, since split SPWM is utilized as the main scheme, conduction and switching losses are relatively low. On the other hand, because joint SPWM is employed for the zero-crossing region, the ac current zero-crossing distortion problem is solved.

The proposed bidirectional ac-dc converter consists of two buck converters under inverter mode, each operating during a half line cycle. As a result, the magnetic components are only utilized during the half line cycle. The low utilization of the magnetic components may impose a serious penalty on system cost and power density. However, the utilization can be improved by integrating the magnetic components. Two
different structures of magnetic integration are presented. One is employing one coupled inductor in series with small inductors and the other one is utilizing two coupled inductors in series.
Chapter 3  Novel Bidirectional AC-DC Converter

3.1  Introduction

A dual-buck converter based bidirectional ac-dc converter was proposed in chapter 2, as shown in Figure 2.5. The circuit consists of two power MOSFETs $a_1$ and $a_2$, two diodes $D_1$ and $D_2$, two inductors $L_1$ and $L_2$, and two split dc bus capacitors $C_1$ and $C_2$. The voltage across each capacitor $C_1$ and $C_2$ should be always larger than the peak ac voltage to ensure the circuit works properly throughout the whole line cycle. The major issues with this type of converter are two large dc bus capacitors, low dc bus voltage utilization, and large-size inductors due to bipolar SPWM control scheme. Also a voltage balance compensator needs to be designed to balance the voltage across the two dc split capacitors.

3.2  Novel Single-Phase Bidirectional AC-DC Converter

3.2.1  Topology

![Figure 3.1  Circuit diagram of the proposed novel single-phase bidirectional ac-dc converter.](image)
To better utilize the dc bus voltage, eliminate the two dc bus capacitors, and reduce the size of the inductors, a novel bidirectional ac-dc converter is derived from Figure 2.5 by replacing the two-capacitor leg with a two-switch leg, as shown in Figure 3.1. The novel bidirectional ac-dc converter keeps the merits of the dual-buck converter based bidirectional ac-dc converter. The converter works as a rectifier when the power is transferred from ac grid to dc source. Alternately, it works as an inverter when the power is transferred from dc source to ac grid.

3.2.2 Operating Principle

Figure 3.2 Operating under rectifier mode with pure active power transferring. (a) Conceptual voltage and current waveform. (b) $a_1$ is on. (c) $D_1$ is on. (d) $a_2$ is on. (e) $D_2$ is on.

Figure 3.2 and Figure 3.3 show the four sub-operating modes under rectifier and inverter modes, respectively. For the rectifier mode with pure active power transferring, there are four sub-operating modes depending on the conducting status of $a_1$, $a_2$, $D_1$, $D_2$, $a_3$, $a_4$, $L_1$, $L_2$, $V_{dc/2}$. 
In the positive current half cycle when \( i_{ac} > 0 \) (\( i_{L2} = 0 \)) and \( v_{ac} < 0 \), leg \( a_1 \) and \( D_1 \) operates and \( a_3 \) is always on. When \( a_1 \) is on and \( D_1 \) is off, current \( i_{ac} \) is increased because the voltage across inductor \( L_1 \) is positive,

\[
V_{L1} = L_1 \frac{di_{ac}}{dt} = v_{ac} > 0 . \tag{3.1}
\]

When \( a_1 \) is off and \( D_1 \) is on, current \( i_{ac} \) is decreased because the voltage across inductor \( L_1 \) is negative,

\[
V_{L1} = L_1 \frac{di_{ac}}{dt} = -\frac{V_{dc}}{2} + v_{ac} < 0 . \tag{3.2}
\]

In the negative current half cycle when \( i_{ac} < 0 \) (\( i_{L1} = 0 \)) and \( v_{ac} > 0 \), leg \( a_2 \) and \( D_2 \) operates and \( a_4 \) is always on. When \( a_2 \) is on and \( D_2 \) is off, current \( i_{ac} \) is increased because the voltage across inductor \( L_2 \) is positive,

\[
V_{L2} = L_2 \frac{di_{ac}}{dt} = v_{ac} > 0 . \tag{3.3}
\]

When \( a_2 \) is off and \( D_2 \) is on, current \( i_{ac} \) is decreased because the voltage across the inductor \( L_2 \) is negative,

\[
V_{L2} = L_2 \frac{di_{ac}}{dt} = -\frac{V_{dc}}{2} + v_{ac} < 0 . \tag{3.4}
\]

Based on the aforementioned analysis, it can be concluded that leg \( a_1 \) and \( D_1 \) and leg \( a_2 \) and \( D_2 \) are controlled by high-frequency SPWM and leg \( a_3 \) and \( a_4 \) is controlled by low-frequency line-cycle signal.

For the inverter mode with pure active power transferring, all the analysis is similar to that of rectifier mode except that the current and voltage are in phase; therefore, the energy is transferred from dc sources to ac grid. In the positive current half cycle when \( i_{ac} > 0 \) (\( i_{L2} = 0 \)) and \( v_{ac} > 0 \), leg \( a_1 \) and \( D_1 \) operates and \( a_4 \) is always on. In the negative current half cycle when \( i_{ac} < 0 \) (\( i_{L1} = 0 \)) and \( v_{ac} < 0 \), leg \( a_2 \) and \( D_2 \) operates and \( a_3 \) is
always on. Based on the aforementioned analysis, it can be concluded that the leg $a_1$ and $D_1$ conducts positive current, and the leg $a_2$ and $D_2$ conducts negative current whenever voltage is positive or negative; $a_3$ is on in the negative voltage half cycle and $a_4$ is on in the positive voltage half cycle whenever current is positive or negative.

To transfer reactive power between ac grid and dc sources, the operation of the circuit becomes much more complicated. Based on the phase angle difference between the ac current and voltage, one line cycle can be represented by four different switch combinations, as shown in Table 3.1, in different order.

**Figure 3.3** Operating under rectifier mode with pure active power transferring. (a) Conceptual voltage and current waveform. (b) $a_1$ is on. (c) $D_1$ is on. (d) $a_2$ is on. (e) $D_2$ is on.

Table 3.1 Different switching combinations

<table>
<thead>
<tr>
<th>Conditions</th>
<th>$a_1$ &amp; $D_1$</th>
<th>$a_2$ &amp; $D_2$</th>
<th>$a_3$</th>
<th>$a_4$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$i_{ac} &gt; 0$ ($i_{L2} = 0$) and $v_{ac} &gt; 0$</td>
<td>PWM</td>
<td>OFF</td>
<td>OFF</td>
<td>ON</td>
</tr>
<tr>
<td>$i_{ac} &gt; 0$ ($i_{L2} = 0$) and $v_{ac} &lt; 0$</td>
<td>PWM</td>
<td>OFF</td>
<td>ON</td>
<td>OFF</td>
</tr>
<tr>
<td>$i_{ac} &lt; 0$ ($i_{L1} = 0$) and $v_{ac} &gt; 0$</td>
<td>OFF</td>
<td>PWM</td>
<td>OFF</td>
<td>ON</td>
</tr>
<tr>
<td>$i_{ac} &lt; 0$ ($i_{L1} = 0$) and $v_{ac} &lt; 0$</td>
<td>OFF</td>
<td>PWM</td>
<td>ON</td>
<td>OFF</td>
</tr>
</tbody>
</table>
3.2.3 Simulation Results

Figure 3.4 Simulation results under (a) rectifier mode and (b) inverter mode.

Figure 3.4(a) and (b) shows the simulation results under both rectifier and inverter modes for the converter, respectively. Figure 3.4(a) shows current and voltage are out of phase. Figure 3.4(b) shows current and voltage are in phase.
3.2.4 Experimental Results

Figure 3.5 Experimental results under (a) rectifier mode and (b) inverter mode.

Figure 3.5(a) and (b) shows the experimental results under both rectifier and inverter modes for the converter, respectively. Figure 3.5(a) shows current and voltage are out of phase. Figure 3.5(b) shows current and voltage are in phase.
3.3 Novel Single-Phase Bidirectional AC-DC Converter with Magnetic Integration

![Diagram of converter operating under rectifier mode]

Figure 3.6 The proposed converter operating under rectifier mode during the period when ac current is positive.

![Diagram of converter operating under rectifier mode]

Figure 3.7 The proposed converter operating under rectifier mode during the period when ac current is negative.

The proposed novel single-phase bidirectional ac-dc converter in Figure 3.1 consists of two boost converters under rectifier mode. One boost converter operates while the other boost converter is inoperative, as shown in Figure 3.6 and Figure 3.7. Each boost converter operates in a half line cycle. Consequently, the magnetic components, $L_1$ and $L_2$, are only utilized in a half line cycle.

Similarly, the novel single-phase bidirectional ac-dc converter in Figure 3.1 consists of two buck converters under inverter mode. One buck converter operates while the other buck converter is inoperative, as indicated in Figure 3.8 and Figure 3.9. Each buck
converter operates in a half line cycle. As a result, the magnetic components, $L_1$ and $L_2$, are only utilized in a half line cycle.

![Diagram](image1)

**Figure 3.8** The proposed converter operating under inverter mode during the period when ac current is positive.

![Diagram](image2)

**Figure 3.9** The proposed converter operating under inverter mode during the period when ac current is negative.

The low utilization of the magnetic components may impose a serious penalty on system cost and power density. However, the utilization can be improved by integrating the magnetic components. The utilization of the magnetic components in Figure 3.1 can be significantly improved by employing different coupled inductor structures. Two different methods of magnetic integration are proposed. One method is to utilize one coupled inductor in series with small inductors and the other one is to employ two coupled inductors in series.
3.3.1 Coupled Inductor in Series with Small Inductors

![Diagram of the novel bidirectional ac-dc converter with one coupled inductor.](image)

**Figure 3.10** Novel bidirectional ac-dc converter with one coupled inductor.

The circuit diagram of the implementation with one coupled inductor is shown in Figure 3.10. In this circuit, two small inductors $L_a$ and $L_b$ are employed to block the undesired circulating current due to the imbalance of the inductance of the coupled inductor.

![Diagram illustrating the proposed converter with one coupled inductor operating under rectifier mode.](image)

**Figure 3.11** The proposed converter with one coupled inductor operating under rectifier mode during the period when ac current is positive.
The proposed magnetic integration method for the bidirectional ac-dc converter in Figure 3.10 consists of two boost converters under rectifier mode. One boost converter operates while the other boost converter is idle, as shown in Figure 3.11 and Figure 3.12. Each boost converter operates in a half line cycle. During the period when ac current is positive, as shown in Figure 3.11, the circuit consists of switch $a_1$, diode $D_1$, inductor $L_a$ and winding $N_A$, and switch $a_3$ operates to conduct the current, while the circuit consists of switch $a_2$, diode $D_2$, inductor $L_b$ and winding $N_B$, and switch $a_4$ is idle. Similarly, as shown in Figure 3.12, during the period when ac current is negative, the circuit consists of switch $a_2$, diode $D_2$, inductor $L_b$ and winding $N_B$, and switch $a_4$ operates to conduct the current, while the circuit consists of switch $a_1$, diode $D_1$, inductor $L_a$ and winding $N_A$, and switch $a_3$ is idle.

The proposed magnetic integration method for the bidirectional ac-dc converter in Figure 3.10 consists of two buck converters under inverter mode. One buck converter operates while the other buck converter is idle, as shown in Figure 3.13 and Figure 3.14. Each buck converter operates in a half line cycle.
In order to analyze the effects of magnetizing and leakage inductance of the coupled inductor on the operation of the bidirectional ac-dc converter under inverter mode in...
Figure 3.13 and Figure 3.14, the coupled inductor with a unity turns ratio is represented with a symmetrical model, as shown in Figure 3.15. In the symmetrical model, each side of the coupled inductor is represented with a magnetizing inductance connected in parallel with the corresponding winding and with a leakage inductance connected in series with the corresponding winding. The value of the magnetizing inductance connected in parallel with each winding of the ideal transformer is twice the total magnetizing inductance of the inductor, $L_{ma} = L_{mb} = 2L_m$.

![Symmetrical model of the proposed novel converter with one coupled inductor under inverter mode.](image)

With voltage and current reference directions under inverter mode as in Figure 3.15, the following voltage relationships can be easily obtained:

\[
\begin{align*}
    v_{a1} &= v_{b1} \quad \text{(3.5)} \\
    v_{a1} &= 2L_m \frac{di_{ma}}{dt} \quad \text{(3.6)} \\
    v_{b1} &= 2L_m \frac{di_{mb}}{dt} \quad \text{(3.7)}
\end{align*}
\]

From (3.5), (3.6) and (3.7), one can obtain

\[
i_{ma} = i_{mb} = i_m \quad \text{(3.8)}
\]
Similarly, with reference to Figure 3.15, the following current relationship can be written:

\[ i_{a1} = -i_{b1} = i_T \]  \hspace{1cm} (3.9)
\[ i_a = i_{ma} + i_{a1} \]  \hspace{1cm} (3.10)
\[ i_b = i_{mb} + i_{b1} . \]  \hspace{1cm} (3.11)

By using (3.8) and (3.9), current \( i_a \) and \( i_b \) can be expressed as:

\[ i_a = i_m + i_T \]  \hspace{1cm} (3.12)
\[ i_b = i_m - i_T . \]  \hspace{1cm} (3.13)

When leg \( a_1 \) and \( D_1 \) is operating and leg \( a_2 \) and \( D_2 \) is idle, one can get \( i_b = 0 \) and \( i_m = i_T \). Apply KVL when \( a_1 \) and \( a_4 \) are on and \( D_1 \) is off as shown in Figure 3.16, the following voltage relationship can be established

\[ \frac{V_{dc}}{2} = (L_a + L_{lka}) \frac{di_a}{dt} + 2L_m \frac{di_{ma}}{dt} + v_{ac}. \]  \hspace{1cm} (3.14)

**Figure 3.16** The proposed novel converter with one coupled inductor operating under inverter mode when ac current is positive and \( a_1 \) and \( a_4 \) are on.
By using (3.8), (3.12) and (3.14), voltage $v_{a1}$ can be expressed as

$$v_{a1} = L_m \frac{di_a}{dt} = \left( \frac{V_{dc} - v_{ac}}{2} \right) \frac{L_m}{(L_a + L_{ka}) + L_m}.$$  \hspace{1cm} (3.15)

Because $a_4$ is on, by using (3.5), the voltage of point B relative to dc negative terminal N can be expressed as

$$0 < V_{BN} = \left( \frac{V_{dc}}{2} - v_{ac} \right) \frac{L_m}{(L_a + L_{ka}) + L_m} + v_{ac} < \frac{V_{dc}}{2}.$$  \hspace{1cm} (3.16)

Obviously, $a_2$ and $D_2$ will never be forced on.

Apply KVL when $a_1$ is off and $D_1$ and $a_4$ are on as shown in Figure 3.17, the following voltage relationship can be obtained

$$0 = (L_a + L_{ka}) \frac{di_a}{dt} + 2L_m \frac{di_{ma}}{dt} + v_{ac}.$$  \hspace{1cm} (3.17)

By using (3.8), (3.12) and (3.17), voltage $v_{a1}$ can be expressed as
Similarly, because $a_4$ is on, the voltage of point B relative to dc negative terminal N can be expressed as

$$0 < V_{BN} = (-v_{ac}) \left(\frac{L_m}{(L_a + L_{i_{ka}}) + L_m} + v_{ac} < v_{ac}\right).$$  (3.19)

Since $v_{ac} < V_{dc}/2$, $a_2$ and $D_2$ will never be forced on.

During the period ac current is negative, leg $a_2$ and $D_2$ is operating and leg $a_1$ and $D_1$ is idle. One can get $i_a = 0$. When $a_2$ and $a_3$ are on and $D_2$ is off, the voltage of dc positive terminal P relative to point A can be expressed as

$$0 < V_{PA} = \left(\frac{V_{dc}}{2} - v_{ac}\right) \left(\frac{L_m}{(L_b + L_{i_{kh}}) + L_m} + v_{ac} < \frac{V_{dc}}{2}\right).$$  (3.20)

Apparently, $a_1$ and $D_1$ will never be forced on.

When $a_2$ is off and $D_2$ and $a_3$ are on, the voltage of dc positive terminal P relative to point A can be expressed as

$$0 < V_{PA} = (0 - v_{ac}) \left(\frac{L_m}{(L_a + L_{i_{ka}}) + L_m} + v_{ac} < v_{ac}\right).$$  (3.21)

Since $v_{ac} < V_{dc}/2$, $a_1$ and $D_1$ will never be forced on.

Same conclusion can be drawn for the converter operating under rectifier mode.

Figure 3.18 (a) and (b) shows the simulation results under both rectifier and inverter modes for the converter, respectively. It can be found that one leg operates while the other is idle.
Figure 3.18 Simulation results of the proposed converter with one coupled inductor under (a) rectifier mode and (b) inverter mode.
Figure 3.19  Experimental results of the proposed converter with one coupled inductor under (a) rectifier mode and (b) inverter mode.

Figure 3.19(a) and (b) shows the experimental results under both rectifier and inverter modes for the converter, respectively.
3.3.2 Two Coupled Inductors in Series

![Diagram](image)

**Figure 3.20** Novel bidirectional ac-dc converter with two coupled inductors.

The other approach of magnetic integration is shown in Figure 3.20. The two inductors $L_1$ and $L_2$ in Figure 3.1 are replaced by two coupled inductors. Although there are still two coupled inductors in the circuit, the size and weight of the inductors are greatly reduced.

![Diagram](image)

**Figure 3.21** The proposed converter with two coupled inductors operating under inverter mode during the period when ac current is positive.
Figure 3.22 The proposed converter with two coupled inductors operating under inverter mode during the period when ac current is negative.

The proposed magnetic integration method for the bidirectional ac-dc converter in Figure 3.20 consists of two buck converters under inverter mode. One buck converter operates while the other buck converter is idle, as shown in Figure 3.21 and Figure 3.22. Each buck converter operates in a half line cycle. During the period when ac current is positive, as shown in Figure 3.21, the circuit consists of switch $a_1$, diode $D_1$, winding $N_{d1}$ and winding $N_{d2}$, and switch $a_4$ operates to conduct the current, while the circuit consists of switch $a_2$, diode $D_2$, winding $N_{b1}$ and winding $N_{b2}$, and switch $a_3$ is idle. Similarly, as shown in Figure 3.22, during the period when ac current is negative, the circuit consists of switch $a_2$, diode $D_2$, winding $N_{b1}$ and winding $N_{b2}$, and switch $a_3$ operates to conduct the current, while the circuit consists of switch $a_1$, diode $D_1$, winding $N_{d1}$ and winding $N_{d2}$, and switch $a_4$ is idle.

The proposed magnetic integration method for the bidirectional ac-dc converter in Figure 3.20 consists of two boost converters under rectifier mode. One boost converter operates while the other boost converter is idle, as shown in Figure 3.23 and Figure 3.24. Each boost converter operates in a half line cycle.
Figure 3.23  The proposed novel converter with two coupled inductors operating under rectifier mode during the period when ac current is positive.

Figure 3.24  The proposed novel converter with two coupled inductors operating under rectifier mode during the period when ac current is negative.

In order to analyze the effects of magnetizing and leakage inductance of the coupled inductor on the operation of the bidirectional ac-dc converter under rectifier mode in
Figure 3.23 and Figure 3.24, the coupled inductor with a unity turns ratio is represented with a symmetrical model, as shown in Figure 3.25. In the symmetrical model, each side of the coupled inductor is represented with a magnetizing inductance connected in parallel with the corresponding winding and with a leakage inductance connected in series with the corresponding winding. The value of the magnetizing inductance connected in parallel with each winding of the ideal transformer is twice the total magnetizing inductance of the inductor.

Figure 3.25 Symmetrical model of the proposed novel converter with two coupled inductors under rectifier mode.

With voltage and current reference directions under rectifier mode as in Figure 3.25, the following voltage relationships can be easily obtained:

\[ v_{a1} = -v_{b1} \]  \hspace{1cm} (3.22)

\[ v_{a2} = v_{b2} \]  \hspace{1cm} (3.23)

\[ v_{a1} = 2L_{m1} \frac{di_{ma1}}{dt} \] \hspace{1cm} (3.24)

\[ v_{b1} = 2L_{m1} \frac{di_{mb1}}{dt} \] \hspace{1cm} (3.25)

\[ v_{a2} = 2L_{m2} \frac{di_{ma2}}{dt} \] \hspace{1cm} (3.26)

\[ v_{b2} = 2L_{m2} \frac{di_{mb2}}{dt} \] \hspace{1cm} (3.27)
From (3.22), (3.24) and (3.25), one can obtain

\[ i_{m_1} = -i_{m_2} = i_{m_1} \]  \hspace{1cm} (3.28)

whereas from (3.23), (3.26) and (3.27)

\[ i_{m_2} = i_{m_2} = i_{m_2}. \]  \hspace{1cm} (3.29)

Similarly, from Figure 3.25, the following current relationship can be written:

\[ i_{a_1} = i_{b_1} \]  \hspace{1cm} (3.30)

\[ i_{a_2} = -i_{b_2} \]  \hspace{1cm} (3.31)

\[ i_a = i_{m_1} + i_{a_1} = i_{m_2} + i_{a_2} \]  \hspace{1cm} (3.32)

\[ i_b = i_{m_1} + i_{b_1} = i_{m_2} + i_{b_2}. \]  \hspace{1cm} (3.33)

Using (3.28) – (3.31) and adding (3.32) and (3.33), it follows that

\[ i_{a_1} = i_{b_1} = i_{m_2} \]  \hspace{1cm} (3.34)

\[ i_{a_2} = -i_{b_2} = i_{m_1}. \]  \hspace{1cm} (3.35)

Also, by using (3.28) and (3.34), current \( i_a \) can be obtained as

\[ i_a = i_{m_1} + i_{m_2} \]  \hspace{1cm} (3.36)

whereas by using (3.28) and (3.34), current \( i_b \) can be obtained as

\[ i_b = -i_{m_1} + i_{m_2} \]  \hspace{1cm} (3.37)
During the positive ac current half cycle, leg $a_1$ and $D_1$ is operating and leg $a_2$ and $D_2$ is idle. When $D_1$ and $a_3$ are on and $a_1$ is off as shown in Figure 3.26, on can get

$$v_{b_1} + v_{b_2} + (L_{lkb1} + L_{lkb2}) \frac{di_b}{dt} = 0.$$  \hspace{1cm} (3.38)

The same result (3.38) also can be obtained when $a_1$ and $a_3$ are on and $D_1$ is off as shown in Figure 3.27.
Similarly, during the negative ac current half cycle, when leg $a_2$ and $D_2$ is operating and leg $a_1$ and $D_1$ is idle, one can get

$$v_{a_1} + v_{a_2} + (L_{a_2} + L_{a_1}) \frac{di_a}{dt} = 0. \quad (3.39)$$

Using (3.25), (3.27), (3.28), (3.29), (3.37) and (3.38), the relationship between $i_{m1}$ and $i_{m2}$ during the positive half line cycle can be expressed as

$$i_{m1} = \frac{L_{m2} + (L_{b1} + L_{b2})/2}{L_{m1} + (L_{b1} + L_{b2})/2} i_{m2}. \quad (3.40)$$

Substituting (3.40) into (3.36) yields

$$i_a = i_{m1} + i_{m2} = \frac{L_{m1} + L_{m2} + (L_{b1} + L_{b2})}{L_{m1} + (L_{b1} + L_{b2})/2} i_{m2}. \quad (3.41)$$

whereas substituting (3.40) into (3.37) yields

$$i_b = -i_{m1} + i_{m2} = \frac{L_{m1} - L_{m2}}{L_{m1} + (L_{b1} + L_{b2})/2} i_{m2}. \quad (3.42)$$

Eliminating $i_{m2}$ from (3.41) and (3.42), the relationship between $i_a$ and $i_b$ can be derived as

$$\frac{i_b}{i_a} = \frac{L_{m1} - L_{m2}}{L_{m1} + L_{m2} + (L_{b1} + L_{b2})}. \quad (3.43)$$

As can be seen from (3.43), for $L_{m1} = L_{m2}$, no ripple current is returned through windings $N_{b1}$ and $N_{b2}$ regardless of their leakage inductance. If $L_{m1} \neq L_{m2}$, the amount of
the ripple current returned through windings $N_{B1}$ and $N_{B2}$ is determined by the difference between the two magnetizing inductances.

Similarly, during the negative ac current half cycle, when leg $a_2$ and $D_2$ is operating and leg $a_1$ and $D_1$ is idle, the relationship between $i_a$ and $i_b$ can be derives as

$$\frac{i_a}{i_b} = \frac{L_{m1} - L_{m2}}{L_{m1} + L_{m2} + (L_{ik1} + L_{ik2})}.$$  

(3.44)

Due to symmetrical operation, the behavior of the circuit during the negative ac current half cycle is identical to that during the positive ac current half cycle.

Under inverter mode during the positive ac current half cycle, when leg $a_1$ and $D_1$ is operating and leg $a_2$ and $D_2$ is idle, the relationship between $i_a$ and $i_b$ can be derives as

$$\frac{i_b}{i_a} = \frac{L_{m1} - L_{m2}}{L_{m1} + L_{m2} + (L_{ik1} + L_{ik2})}.$$  

(3.45)

Under inverter mode during the negative ac current half cycle, when leg $a_2$ and $D_2$ is operating and leg $a_1$ and $D_1$ is idle, the relationship between $i_a$ and $i_b$ can be derives as

$$\frac{i_a}{i_b} = \frac{L_{m1} - L_{m2}}{L_{m1} + L_{m2} + (L_{ik1} + L_{ik2})}.$$  

(3.46)

Due to symmetrical operation, the behavior of the circuit under inverter mode is identical to that under rectifier mode.

The two separate inductors, $L_1$ and $L_2$, are shown in Figure 3.28. Each inductor consists of four 77192 Kool Mu cores and two paralleled litz wires (22 turns, AWG #14). Figure 3.29 shows the structure of the two coupled inductors. Each coupled inductor consists of two 77192 Kool Mu cores. Two paralleled litz wires (22 turns, AWG #14) are used for each winding of $N_{A1}$, $N_{B1}$, $N_{A2}$, and $N_{B2}$.
Figure 3.28  Picture of the constructed separate inductors.

Figure 3.29  Picture of the constructed two coupled inductors.

Figure 3.30(a) and (b) shows the simulation results under both rectifier and inverter modes for the converter, respectively. It can be concluded that one leg operates while the other leg is idle.
Figure 3.30 Simulation results of the proposed converter with two coupled inductors under (a) rectifier mode and (b) inverter mode.
Figure 3.31 Experimental results of the proposed converter with two coupled inductors under (a) rectifier mode and (b) inverter mode.

Figure 3.31(a) and (b) shows the experimental results under both rectifier and inverter modes for the converter, respectively.
3.4 Novel Three-Phase Bidirectional AC-DC Converter

Three-phase ac-dc conversion of electric power is widely employed in motor drive, uninterruptible power supplies, and utility interfaces with renewable sources such as solar photovoltaic, wind and battery energy storage systems. Numerous three-phase topologies that have bidirectional flow capability have been reported [65]-[84]. The commonly used bidirectional converter topology consists of six power switches as shown in Figure 3.32. Without neutral connection, third harmonic will not exist. There is no need to need to eliminate 3rd, 9th, etc. triplen harmonics. For this topology, the power MOSFET cannot be used as the main switch in the high-voltage high-power applications because the intrinsic MOSFET body diode conduction could cause device failure.

![Figure 3.32 Circuit diagram of the traditional three-phase six-switch bidirectional ac-dc converter.](image)

Figure 3.33(a) and (b) show the sub-operating modes under inverter mode for one switching cycle. When $S_1$, $S_6$ and $S_2$ are on as shown in Figure 3.33(a), all diodes are off. When $S_1$ is off, Current $i_a$ goes through anti-parallelled diode of $S_4$ as shown in Figure 3.33(b). In this case, if $S_4$ is replaced by a power MOSFET, the body diode of $S_4$ will conduct the current. Even if $S_4$ works under synchronous rectification when $S_1$ is off, the body diode of $S_4$ will conduct the current during the dead time. Excessive reverse recovery loss of the body diode could cause device failure.
The power MOSFET cannot be used as the main switch in the three-phase converter since the intrinsic MOSFET body diode conduction could cause device failure. However, an IGBT has higher switching and conduction losses compared with a power MOSFET. In addition, the IGBT only allows operation at a lower switch frequency than the power MOSFET which results in larger filter size. On the contrary, lots of revolutionary technology has been employed for the high-voltage power MOSFET, which make the MOSFET’s $R_{DS_{on}}$ exceptionally low. Extremely low switching and conduction losses make switching applications even more efficient, more compact, lighter and cooler.

In this section, three MOSFET based novel three-phase bidirectional ac-dc converters are proposed.

---

**Figure 3.33** Operating under inverter mode for one switching cycle. (a) $S_1, S_6$ and $S_2$ are on. (b) Diode of $S_4, S_6$ and $S_2$ are on.
3.4.1 Novel Three-Phase Bidirectional AC-DC Converter Topologies

A novel three-phase bidirectional ac-dc converter is proposed in Figure 3.34. The converter is based on the dual-buck based single-phase bidirectional ac-dc converter, which is shown in Figure 2.5.

The converter exhibits two distinct merits: first, there is no shoot-through issue because no active power switches are connected in series in each phase leg; second, the reverse recovery dissipation of the power switch is greatly reduced because there is no freewheeling current flowing through the body diode of power switches. Using MOSFET as the main device, not only can the switching loss be almost eliminated but also the conduction loss can be significantly reduced. Besides the features of the single-phase dual-buck converter, the three-phase converter eliminates the two bulky dc bus capacitors and related voltage-balancing control algorithm.

The converter works as a rectifier when the power is transferred from ac grid to dc source. Alternately, it works as an inverter when the power is transferred from dc source to ac grid.
A novel three-phase converter with split capacitors for neutral connection is shown in Figure 3.35. Under unbalanced ac load condition, dc bus capacitors absorb the neutral current to maintain better balanced ac output. The problem with this topology is excessive current stress on split capacitors when ac load are highly unbalanced.

Figure 3.35  Circuit diagram of a novel three-phase bidirectional ac-dc converter with split capacitors for neutral connection.

Figure 3.36  Circuit diagram of a novel three-phase bidirectional ac-dc converter with extra leg.
A novel three-phase four-leg converter is shown in Figure 3.36. Neutral leg is controlled to equalize the three-phase outputs. The features with this converter are less bulky capacitors and reduced size of passive components. However, control is more complicated.

### 3.4.2 Operating Principle

The definition of the different power transferring modes based on phase angle difference between voltage and current waveforms for single-phase bidirectional ac-dc converter are shown in Figure 2.6. The same definition is also applied for the three-phase bidirectional ac-dc converters.

![Ideal three-phase current waveforms](image)

**Figure 3.37** Ideal three-phase current waveforms.

The ideal three-phase current waveforms are shown in Figure 3.37. One ac line cycle is divided into six regions. In region $0^\circ$–$60^\circ$, $120^\circ$–$180^\circ$, and $240^\circ$–$300^\circ$, the current waveform in Figure 3.37 have the same pattern, i.e., two phases have current amplitudes higher than that of the other one. In region $60^\circ$–$120^\circ$, $180^\circ$–$240^\circ$, and $300^\circ$–$360^\circ$, the current waveform in Figure 3.37 have the same pattern, i.e., two phases have current amplitudes lower than that of the other one.
One switching cycle for the converter shown in Figure 3.34 under inverter mode when the phase angle is between 60° and 120° is analyzed as an example. Figure 3.38 shows the gate signals and related sub-operating modes.

In mode 1, \( D_1, b_2 \) and \( b_3 \) are on. There is no power transferred between dc side and ac side. The currents are freewheeling within the three phases. In mode 2, \( a_1, b_2 \) and \( b_3 \) are on. The power is transferred from dc side to ac side. In mode 3, \( a_1, D_4 \) and \( D_6 \) are on. There is no power transferred between dc side and ac side. The currents are freewheeling within the three phases. Mode 4 is the same as mode 2 and Mode 5 is the same as mode 1.

### 3.4.3 Simulation Results

Figure 3.39(a) and (b) shows the simulation results under both rectifier and inverter modes for the converter shown in Figure 3.34, respectively.

Figure 3.40(a) and (b) show simulated waveforms with reactive power flow for the converter shown in Figure 3.34. Figure 3.40(a) shows current leads voltage by 90°. Figure 3.40(b) shows current lags voltage by 90°.
Figure 3.39 Simulation results under (a) rectifier mode and (b) inverter mode.
Figure 3.40  Simulation results with reactive power flow. (a) Current leads voltage by 90°. (b) Current lags voltage by 90°.
3.5 Summary

To better utilize the dc bus voltage and eliminate the two dc bus capacitors, a novel bidirectional ac-dc converter is proposed by replacing the two-capacitor leg of the dual-buck converter based single-phase bidirectional ac-dc converter with a two-switch leg. The novel bidirectional ac-dc converter keeps the merits of the dual-buck converter based bidirectional ac-dc converter. Meanwhile the two large dc bus capacitors and related voltage-balancing control are eliminated. The converter works as a rectifier when the power is transferred from ac grid to dc source. Alternately, it works as an inverter when the power is transferred from dc source to ac grid.

The novel bidirectional ac-dc converter consists of two boost converters under rectifier mode, each operating during a half line cycle. It consists of two buck converters under inverter mode, each operating during a half line cycle. As a result, the magnetic components are only utilized during the half line cycle. The low utilization of the magnetic components may impose a serious penalty on system cost and power density. However, the utilization can be improved by integrating magnetic components. Two different structures of magnetic integration are presented. One is employing one coupled inductor in series with small inductors and the other one is utilizing two coupled inductors in series.

Three novel three-phase bidirectional ac-dc converter topologies are proposed. They keep the merits of the novel single-phase bidirectional ac-dc converter. Detailed operating principles are described.

Overall, a novel single-phase bidirectional ac-dc converter is proposed. With magnetic integration, the total number of the magnetic cores is reduced by half with the same converter efficiency. Based on the single-phase bidirectional ac-dc converter topology, three novel three-phase bidirectional ac-dc converter topologies are proposed.
Chapter 4 Unified Controller for Bidirectional Power Flow Control

4.1 Introduction

The dual-buck converter based single-phase bidirectional ac-dc converter was proposed in chapter 2. With magnetic integration, the power density is significantly improved and the weight of the converter is reduced. In this chapter, the modeling of the power stage is described.

The analog control implementation intends to have difficulties during the mode transition, because the error amplifier of the preferred mode can be saturated during the transition. Digital controller can be easily set to reduce or avoid the delay out of the saturation in the transition.

In order to control the bidirectional power flow and at the same time stabilize the system in mode transition, a unified digital controller is described in this chapter. The basic concept of a unified controller is explained. An admittance compensator along with a QPR controller is adopted to allow smooth startup and elimination of the steady-state error over the entire load range. Both simulation and experimental results match very well and validate the design of the proposed unified controller.

4.2 Unified Controller Concept

Figure 4.1 shows the traditional method of two separate controllers: one for rectifier mode and the other one for inverter mode. The current references $i_{ac\_rec}^*$ and $i_{ac\_inv}^*$ are provided by the power management command separately. The mode switch between two different modes is controlled by the mode selection command. To achieve the mode transition, the converter has to gradually decrease the current to zero under one controller and then gradually increase the current to the desired value under the other controller.
Figure 4.1 Separate controller controlled system.

Figure 4.2 Unified controller controlled system.
Instead of individual controllers for each mode shown in Figure 4.1, a unified controller is proposed in Figure 4.2. For the unified controller, the reference is controlled by the parameter $\theta$, which is defined as the phase angle difference between ac current and voltage shown in Figure 2.6. When $\theta = 0$, the ac current is controlled to have the same phase angle relative to the voltage. The converter operates under inverter mode. When $\theta = 180$, the ac current is controlled to have the 180° phase shift relative to the voltage. The converter operates under rectifier mode.

\[
i_{ac} \quad v_{ac}
\]

\[
L_1 \quad C_1
\Rightarrow
\begin{align*}
D_1 & \quad D_2 \\
a_1 & \quad a_2
\end{align*}
\]

From Figure 4.3(b) and (c), when current is positive in the rectifier mode, the total volt-seconds applied to the inductor $L_1$ over one switching period are

\[
\left(\frac{V_{dc}}{2} + v_{ac}\right) \cdot d_{a_1\_rec} + \left(-\frac{V_{dc}}{2} + v_{ac}\right) \cdot (1 - d_{a_1\_rec}) = 0. \quad (4.1)
\]

The duty cycle for switch $a_1$ can be derived as
\[ d_{a1_{\text{rec}}} = \frac{1}{2} (1 - \frac{v_{ac}}{V_{dc}}) = \frac{1}{2} (1 - \frac{v_{pk} \sin \omega t}{V_{dc}/2}) = 0.5 \cdot (1 - M \sin \omega t) . \] (4.2)

where \( M = \frac{v_{pk}}{(V_{dc}/2)} \) is modulation index and \( \sin \omega t > 0 \). Similarly, the duty cycle for switch \( a_2 \) in the rectifier mode can be derived as

\[ d_{a2_{\text{rec}}} = 0.5 \cdot (1 + M \sin \omega t) . \] (4.3)

![Diagram](image_url)

**Figure 4.4** Operating under inverter mode with pure active power transferring. (a) Conceptual voltage and current waveform. (b) \( a_1 \) is on. (c) \( D_1 \) is on.

From Figure 4.4(b) and (c), when current is positive in the inverter mode, the total volt-seconds applied to the inductor \( L_1 \) over one switching period are

\[ (\frac{V_{dc}}{2} - v_{ac}) \cdot d_{a1_{\text{rec}}} + (\frac{V_{dc}}{2} - v_{ac}) \cdot (1 - d_{a1_{\text{rec}}}) = 0 . \] (4.4)

The duty cycle for switch \( a_1 \) can be derived as

\[ d_{a1_{\text{inv}}} = 0.5 \cdot (1 + M \sin \omega t) . \] (4.5)
where $M = \frac{v_{pk}}{(V_{dc}/2)}$ is modulation index and $\sin \omega t > 0$. Similarly, the duty cycle for switch $a_2$ in the inverter mode can be derived as

$$d_{a_2\_inv} = 0.5 \cdot (1 - M \sin \omega t). \quad (4.6)$$

It can be concluded that $d_{a_1\_rec} = -d_{a_1\_inv}$ and $d_{a_2\_rec} = -d_{a_2\_inv}$. By changing the phase angle $\theta$ from $180^\circ$ to $0^\circ$, current reference is changed from $i_{ac}^*$ to $-i_{ac}^*$. The control output applied to $d_{a_1}$ to conduct positive current under rectifier mode will also be used for $d_{a_1}$ to conduct positive current under inverter mode. The control output applied to $d_{a_2}$ to conduct negative current under rectifier mode will also be used for $d_{a_2}$ to conduct negative current under inverter mode. One controller can be used to regulate current under both rectifier and inverter modes by adjusting the phase angle $\theta$.

### 4.3 Unified Controller Design

#### 4.3.1 Modeling of the Power Stage

The approach of modeling the dual-buck converter based single-phase bidirectional ac-dc converter is the same as the traditional full-bridge dc-ac inverter with bipolar PWM control. Assume the two inductors have the same inductance and the equivalent series resistance (ESR) is $r$ in Figure 4.5, the following voltage relationships can be easily obtained:

$$r i_{ac} (t) + L \frac{di_{ac}(t)}{dt} = \frac{V_{dc}}{2} \cdot d - v_{ac}\cdot \quad (4.7)$$

The output current $i_{ac}$ can be derived as

$$i_{ac}(s) = \frac{V_{dc}/2}{r + sL} \cdot d - \frac{1}{r + sL} \cdot v_{ac} = G_{sd}(s) \cdot d - G_{rs}(s) \cdot v_{ac}. \quad (4.8)$$

where
\[ G_{id}(s) = \frac{i_{ac}(s)}{d(s)} = \frac{V_{dc}/2}{r + sL} \] (4.9)

is the control-to-output transfer function, and

\[ G_{iv}(s) = \frac{i_{ac}(s)}{v_{ac}(s)} = \frac{1}{r + sL} \] (4.10)

is the current-to-voltage transfer function, which is uncontrolled feed-forward term.

Figure 4.5 shows the complete circuit diagram that includes a current-loop controller. Current command \(i_{ref}\) is obtained from the active power reference \(P_{ref}\) and the reactive power reference \(Q_{ref}\), which are commanded by the power management, and the ac voltage phase information, which is produced by a digital phase-locked loop (PLL).
Figure 4.6 shows the block diagram of the compensated system that adds $G_i(s)$. $H_v(s)$ and $H_i(s)$ are voltage and current sensor gains. The current loop controller $G_i(s)$ is designed to compensate the error $i_{err}$ between $i_{ref}$ and the feedback sensed current $i_{fb}$. By feeding the output of the current loop controller to the PWM block, which is represented by $F_m$, the output signal is gating signal $d$.

4.3.2 Unified Controller Design

From Figure 4.6, the overall equivalent admittance can be represented as

$$Y(s) = \frac{i_{ac}(s)}{v_{ac}(s)} = \frac{I_m H_v G_i(s) F_m G_{id}(s)}{1 + T_i} = Y_1(s) + Y_2(s)$$  \hspace{1cm} (4.11)$$

where $T_i(s) = G_i(s) F_m G_{id}(s) H_i$ is the loop gain, $Y_1(s) = [I_m H_v G_i(s) F_m G_{id}(s)]/(1+T_i(s))$, and $Y_2(s) = -G_{iv}(s)/(1+T_i(s))$.

The active and reactive power reference command can be used to calculate $I_m$ and $\theta$ shown as

$$I_m = \sqrt{\frac{P_{ref}^2 + Q_{ref}^2}{v_{ph}^2 / 2}}$$  \hspace{1cm} (4.12)$$

$$\theta = \tan^{-1}\left(\frac{Q_{ref}}{P_{ref}}\right)$$  \hspace{1cm} (4.13)$$
The term \( Y_1(s) \) is generated by active and reactive power reference command \( P_{ref} \) and \( Q_{ref} \), which provides desired output. The term \( Y_2(s) \) is related to the closed-loop voltage-to-current transfer function, which reduces current induced in \( Y_1 \). Thus, \( Y_2 \) is undesired and needs to be eliminated by the use of the adding admittance compensator \( G_c(s) \) shown in Figure 4.7 [82]-[84].

\[
\begin{align*}
\text{Figure 4.7} & \quad \text{Block diagram of the current control loop with the adding admittance compensator.} \\
\text{Figure 4.8} & \quad \text{Block diagram of the current control loop with the adding admittance compensator for derivation.}
\end{align*}
\]

Since \( G_c(s) \) is used to cancel the term \( Y_2(s) \), it can be easily derived from Figure 4.8 as

\[
G_c(s) = \frac{G_v(s)}{F_m G_{id}(s)} = \frac{1}{F_m (V_{dc}/2)}. \tag{4.14}
\]
Equation (4.14) indicates that $G_c(s)$ is independent of converter transfer functions and proportional with the multiplicative inverse of the half dc bus voltage $V_{dc}/2$ and the PWM gain $F_m$.

$$G_c(s) = \frac{1}{V_{dc}/2 F_m}$$

Figure 4.9 shows the complete circuit diagram that includes $G_i(s)$, $G_{vb}(s)$ and $G_c(s)$. The voltage balance compensator $G_{vb}(s)$ is designed to balance the voltage across the two dc split capacitors, $v_{c1}$ and $v_{c2}$. The admittance compensator $G_c(s)$ is designed to reject the disturbance from $G_{iv}(s)$.

In order to reduce the steady-state error at the fundamental frequency, or 60 Hz in the designed case, the QPR controller, which is shown in (4.15), is adopted for the current loop controller $G_i(s)$, which can provide a high gain at 60 Hz without phase offset [81].

$$G_i(s) = k_p + \frac{2k_c \omega_r s}{s^2 + 2\omega_c s + \omega_0^2}.$$  \hspace{1cm} (4.15)
Here, $k_p$ is a proportional gain, $k_r$ is a resonant gain, and $\omega_c$ is an equivalent bandwidth of the resonant controller. The QPR controller is designed to have the following parameters: $k_p = 1.5$, $k_r = 50$, $\omega_c = 10$ rad/s, and $\omega_o = 2\pi \times 60$ rad/s.

A proportional-integral (PI) controller, which is shown in (4.16), is adopted to balance the voltage across the two dc split capacitors, $v_{c_1}$ and $v_{c_2}$. $k_p$ is designed as small as possible to have less influence on the main control loop, and $k_i$ is designed to have large time constant. In this design, $k_p = 0.6$ and $k_i = 60$.

$$G_{vb}(s) = k_p + \frac{k_i}{s}. \quad (4.16)$$

![Figure 4.10 Bode plot of the compensated loop gain $T_i(s)$.](image)
Using the above current loop controller and system parameters, the compensated loop gain $T_i(s) = G_i(s)F_mG_{id}(s)H_i$ is plotted in Figure 4.10. As shown in the bode plot, the crossover frequency and phase margin are 2.75 kHz and 84.9°, respectively.

### 4.3.3 Discretization of the QPR current controller

The current controller $G_i(s)$ obtained above has two parts: a proportional controller and a resonant controller shown in (4.17). Since the proportional controller is just a gain, this section focuses on the discretization of the resonant controller.

$$G_{i\text{ - resonant}}(s) = \frac{2k_r\omega_c s}{s^2 + 2\omega_c s + \omega_o^2} \tag{4.17}$$

where $k_r = 50$, $\omega_c = 10$ rad/s, and $\omega_o = 2\pi \times 60$ rad/s.

The trapezoidal integration based Z-transform shown in (4.18), also known as Tustin transform, is utilized because it preserves stability and minimum-phase for both gain and phase properties of the controller below one tenth of the sampling frequency.

$$s = \frac{2}{T_s} \frac{z - 1}{z + 1} \tag{4.18}$$

where $T_s = 20 \mu$s is sampling time.

Substituting the $s$ variable in (4.17) with the expression indicated in (4.18), it can be found

$$G_{i\text{ - resonant}}(Z) = \frac{a_2 z^2 + a_1 z + a_0}{b_2 z^2 + b_1 z + b_0} \tag{4.19}$$

where $a_2 = 0.00999786$, $a_1 = 0$, $a_0 = -0.00999786$, $b_2 = 1$, $b_1 = -1.99954325$, and $b_0 = 0.99960001$. Figure 4.11 represents a detailed description of the designed digital resonant converter.
In order to implement a controller on a FPGA, the controller coefficients must be truncated (or rounded) into certain word length binary representation, so as to be fit to the numbers of bits available to the FPGA for variables and constants. In general, the effect of coefficient result truncation (or rounding) leads to the shift of the system zeros and poles and therefore a distortion of the controller’s frequency response.

The corresponding truncated coefficients are expressed as
\[ G_{\text{resonant quantization}}(Z) = \frac{c_2 z^2 + c_1 z + c_0}{d_2 z^2 + d_1 z + d_0}. \]  

(4.20)

where \( c_2 = 328, c_1 = 0, c_0 = -328, d_2 = 32768, d_1 = -65521, \) and \( d_0 = 32755. \) The digital implementation of the resonant controller in FPGA and Simulink is indicated in Figure 4.12.

The Bode plots of the analog controller described in (4.17), the digital controller described in (4.19), and the digital controller with truncation described in (4.20), are shown in Figure 4.13. As can be seen, the analog and digital controllers are almost overlapped by each other. The two resonant poles of the truncated digital controller are shifted from 60 Hz to 62.18 Hz.

The frequency response magnitudes of the analog controller, the digital controller, and the digital controller with truncation, are shown in Figure 4.14. As can be seen, the frequency response magnitude of the analog controller has a peak value of 50 at 60 Hz.
However, the peak points for the digital and truncated digital controller are shifted. The frequency response magnitude is 37.35 for the digital controller and 35.57 for the truncated digital controller at 60 Hz.

![Comparison of Frequency Response Magnitudes](image)

Figure 4.14 Comparison of frequency response magnitudes of the analog controller, the digital controller, and the digital controller with truncation.

### 4.4 Simulation Results

Two different simulation tools, PSIM and Simulink, are used to verify the operation of the dual-buck converter based single-phase bidirectional ac-dc converter.

#### 4.4.1 PSIM Simulation

![Power stage in PSIM](image)

Figure 4.15 Power stage in PSIM.
Figure 4.16  Control circuit in PSIM.

Figure 4.15 and Figure 4.16 show the power stage and control circuit in PSIM, respectively. In the PSIM simulation, the system is considered as continuous-time system since the digital controller and analog-to-digital converter (ADC) are not used.

Figure 4.17(a) and (b) shows the PSIM simulation results under both rectifier and inverter modes for the converter, respectively.
Figure 4.17 Simulation results under (a) rectifier mode and (b) inverter mode, both with $v_{ac} = 30 \, V_{rms}$ and $i_{ac} = 28 \, A_{rms}$.

4.4.2 Simulink Simulation

Figure 4.18 Power stage in PSIM.
Although digital controller can be implemented in PSIM, Simulink is preferred to implement the controller for its capability of model-based design and multi-domain simulation.

Here are the steps to build the circuit in Simulink. First, the power stage circuit is built in PSIM, which is shown in Figure 4.18. Second, the power stage circuit built in PSIM is created as a model block in Simulink. Also, the digital control circuit is built in Simulink as shown in Figure 4.19. Finally, the power stage block and the digital control circuit are connected in Simulink. The sampling and computational delays with digital control are unavoidable and also considered in the simulation.

As can be seen from Figure 4.19, the circuit consists of a power stage block from PSIM, ADC, digital controller, and digital PWM module. All the modules are synchronized by a 50 kHz clock, which is set as the switching frequency. The control parameters in the Simulink simulation can be directly used in the FPGA code implementation.

**Figure 4.19 Control circuit in Simulink.**
Figure 4.20 Simulation results under (a) rectifier mode and (b) inverter mode, both with $v_{ac} = 30 \text{ V}_{\text{rms}}$ and $i_{ac} = 28 \text{ A}_{\text{rms}}$.

Figure 4.20(a) and (b) shows the Simulink simulation results under both rectifier and inverter modes for the converter, respectively.
4.5 Experimental Results

Figure 4.21 Experimental results of seamless energy transfer. (a) Changing from rectifier mode to inverter mode at the peak current point. (b) Changing from inverter mode to rectifier mode at the peak current point.
For the experiment, the bidirectional ac-dc converter is connected between the batteries and ac grid. Figure 4.21(a) shows transient waveforms from rectifier mode to inverter mode in 40 µs when the battery pack has a SOC value of around 70%. Figure 4.21(b) shows transient waveforms from inverter mode to rectifier mode in 40 µs when the battery pack has a SOC value of around 70%. These waveforms show seamless energy transfer.

4.6 Summary

In order to control the bidirectional power flow and at the same time stabilize the system in mode transition, a unified digital controller is proposed in this chapter. The basic concept of a unified controller is explained. The differences between individual controllers and unified controller are described.

The power stage small-signal model is derived for the dual-buck converter based single-phase bidirectional ac-dc converter. Based on the small-signal model, an admittance compensator along with a QPR controller is adopted to allow smooth startup and elimination of the steady-state error over the entire load range. The proposed QPR controller is designed and implemented with a digital controller. Then the coefficients of the digital controller are truncated into certain word length binary representation, so as to be fit to the numbers of bits available to the FPGA for variables and constants. The characteristics of the designed analog resonant controller, digital controller, and truncated digital controller are analyzed. The frequency responses of the three controllers are also obtained.

The entire system has been simulated in both PSIM and Simulink and verified with hardware experiments. Small transient currents are observed with the power transferred from rectifier mode to inverter mode at peak current point and also from inverter mode to rectifier mode at peak current point.
Chapter 5  Grid-Tie Battery Energy Storage System Design

5.1 Introduction

Recent developments in lithium-ion battery technology show many advantages compared to lead-acid, nickel-metal hydride and nickel-cadmium batteries, such as high open circuit voltage, low self-discharge rate, high power and energy density, and high charge-discharge efficiency [23]-[27].

![Circuit diagram of a lithium-ion battery energy storage system](image)

Figure 5.1  Circuit diagram of a lithium-ion battery energy storage system

As indicated in Figure 5.1, a battery energy storage system consists of three subsystems, a LiFePO$_4$ battery pack and associated BMS, a bidirectional ac-dc converter, and the central control unit which controls the operation mode and grid interface of the energy storage system. The BMS controller monitors the parameters of each battery cell,
such as cell voltage, temperature, charging and discharging current; estimates the SOC and SOH of each battery cell in the pack. The SOC information is then used to control the charge equalization circuits to mitigate the mismatch among the series connected battery cells. The SOC and SOH information is also used by the central control unit to determine the operating mode of the energy storage system. The bidirectional ac-dc converter works as the interface between the battery pack and the ac grid, which needs to meet the requirements of bidirectional power flow capability and to ensure high power factor and low THD as well as regulate the dc side power regulation.

In the previous chapters, novel bidirectional ac-dc converter topologies and related control schemes are proposed. The dual-buck converter based single-phase bidirectional ac-dc converter is proposed in chapter 2. To better utilize the dc bus voltage and eliminate the two dc bus capacitors, a novel bidirectional ac-dc converter is proposed by replacing the two-capacitor leg with a two-switch leg in chapter 3. In order to control the bidirectional power flow and at the same time stabilize the system in mode transition, a unified digital controller is proposed in chapter 4. This chapter will focus on the grid-tie battery energy storage system design and implementation.

### 5.2 Battery Management System Configuration

In a Lithium-ion battery system, BMS is the key component to ensure all cell voltages being strictly kept in boundaries for safety operation and cycle life. There are two key functions in the designed BMS: monitoring and charge equalization.

First, the BMS monitors the status of all the series connected lithium-ion battery cells in the system. The parameters being monitored includes cell voltage, cell temperature, charging and discharging current. The voltage measurements are performed by an analog front end integrated circuit, which is able to select and level shift the voltage across any of 12 stacked battery cells. All the signals are multiplexed to a differential analog to digital converter to convert into digital domain. The voltage, current and temperature information are then processed by the BMS controller to determine the SOC, SOH and capacity of each battery cell, and protect all the cells operate in the designed SOC range.

Second, the designed BMS applies active balancing to equalize the cells in the pack. In a Lithium-ion battery system, all cell voltages need to be strictly kept in boundaries to
ensure safety operation. However, due to production deviations, inhomogeneous aging and temperature difference within the battery pack, there are SOC or capacity imbalances between battery cells. Minimize the mismatches across all the cells are important to guarantee the power or energy performance of the pack, as they are limited by first cell which goes beyond the boundaries. In this system, an inductive based active cell balancing approach is used to regulate the amount of charge in and out of each individual cell to balance the mismatches across the cell to maintain the homogeneous status across the battery pack.

Figure 5.2 Proposed BMS configuration.
Figure 5.2 shows the configuration of the proposed BMS. It consists of module controllers, which manage up to twelve series connected battery cells, and central controller which manages the series connected battery modules, reports cell status and control the relays to protect the battery pack from over-charging or under-charging conditions. High voltage isolated CAN bus is used to communicate between the module controllers and central controller.

5.3 SOC Estimation

<table>
<thead>
<tr>
<th>Technique</th>
<th>Summarized Features</th>
<th>Pros</th>
<th>Cons</th>
</tr>
</thead>
<tbody>
<tr>
<td>Discharge</td>
<td>Discharge with DC current and measure time to a certain threshold</td>
<td>Most accurate</td>
<td>Offline, Time consuming</td>
</tr>
<tr>
<td>Coulomb counting</td>
<td>Counting charges that have been injected/pumped out of battery</td>
<td>Online, Easy</td>
<td>Loss model, Need accuracy</td>
</tr>
<tr>
<td>Open circuit voltage</td>
<td>VOC-SOC look-up table</td>
<td>Online, Accurate</td>
<td>Time consuming</td>
</tr>
<tr>
<td>Artificial neural network</td>
<td>Adaptive artificial neural network system</td>
<td>Online</td>
<td>Training data needed</td>
</tr>
<tr>
<td>Impedance</td>
<td>Impedance of the battery (RC combination)</td>
<td>Online, SOC and SOH</td>
<td>Cost, Temp-sensitive</td>
</tr>
<tr>
<td>DC resistance</td>
<td>$R_{dc}$</td>
<td>Online, Easy</td>
<td>Cost, Temp-sensitive</td>
</tr>
<tr>
<td>Kalman filter</td>
<td>Get accurate information out of inaccurate data using Kalman filter</td>
<td>Online, Dynamic</td>
<td>Large computing, Model needed</td>
</tr>
</tbody>
</table>

SOC is a measure of the amount of electrochemical energy left in a cell or battery. It is expressed as a percentage of the battery capacity and indicates how much charges (energy) stored in an energy storage element. It has been a long-standing challenge for battery
industry to precisely estimate the SOC of lithium-ion batteries. The electrochemical reaction inside batteries is very complicated and hard to model electrically in a reasonably accurate way. So far, the state-of-the-art SOC accuracy for electric vehicle/plug-in hybrid EV (EV/PHEV) applications is in the range of 5%-10% [35]-[38].

Table 1.1 shows the comparison of different SOC estimation schemes. Among all the practical techniques, the Coulomb counting plus an accurate open-circuit voltage model is the algorithm being used here to estimate the SOC.

First, the initial SOC of the battery cell is established from look-up tables. The table consists of open circuit voltage and corresponding SOC information. An initial charge and discharge test cycle is necessary to generate such a look-up table. In the test cycle, the battery cell will perform a full 0.1C charging and discharging cycle. Two open circuit voltages, $V_{\text{charge}}$ and $V_{\text{discharge}}$, versus SOC curves are plotted and the open circuit voltage (VOC) will be the average of the $V_{\text{charge}}$ and $V_{\text{discharge}}$, as shown in Figure 5.3(a). This process will be repeated at different temperatures to generate a set of look-up tables to accommodate different temperature situations, as shown in Figure 5.3(b).

Figure 5.3 (a) Open circuit voltage versus SOC curve. (b) SOC look-up tables for different temperatures.
Then, a Coulomb counter is initiated to count how many Coulombs of charge being pumped into or out of the battery cell. The Coulomb counter consists of an accurate battery current sense analog front end as well as a digital signal processing unit to perform the offset calibration as well as charge integration for coulomb counting purpose. Coulomb counting provides higher accuracy than most other SOC measurements since it measures the charge flow in and out of battery cell directly. However, it depends on the accuracy of the current measurement and does not take account of Columbic efficiency of the battery cell. Therefore, an accurate loss model is desired and necessary. The loss comes from different mechanisms, which includes physical resistance of the cathode, anode, metal materials, the lithium ion diffusion loss, as well as other chemical reaction thermal loss. An accurate model to include all these mechanisms is difficult to establish in reality. Hereby a combination of Coulomb counting with SOC adjustment by open circuit voltage look-up table method is applied. During battery charging or discharging, Coulomb counting is used to estimate the change of SOC for its accurate measurement of direct charge flow. The SOC of start and end of charging or discharging is being calibrated by using open circuit voltage look up table. This method combines the advantage of relative higher accuracy of both Coulomb counting and open circuit voltage, but mitigate the slow response time of open circuit voltage scheme and lacking relative reference point of Coulomb counting method.

5.4 Charge Equalization

Due to inevitable differences in chemical and electrical characteristics from manufacturing, aging, and ambient temperatures, there are SOC or capacity imbalances between battery cells. When these unbalanced batteries are left in use without any control, such as cell equalization, the energy storage capacity decreases severely. Thus, charge equalization for a series connected battery string is necessary to minimize the mismatches across all the cells and extend the battery lifecycle. Charge balancing methods can be classified into two categories: active and passive.

Active cell balancing helps balance the cells in a battery module to maintain the same voltage or SOC by monitoring and injecting appropriate balancing current into individual battery cell based on the balancing scheme. Compared with the traditional passive cell
balancing approach, the active cell balancing offers the advantage of high system efficiency and fast balancing time.

An inductive based active cell balancing scheme similar to the design in [27] is applied in this work to perform the cell equalization and mitigate the SOC mismatches among the cells. The unidirectional dc-dc converter is replaced by an isolated bidirectional dc-dc converter. The isolated bidirectional dc-dc converter regulates from the 12 cell battery stack voltage to each individual cell voltage. The average current mode control is employed such that the average inductor current is regulated to the command current which is set by the active cell balancing control algorithm. The voltage measurement circuit senses and converts all cell voltages into digital domain. Depend on the active cell balancing control algorithm, the battery cells could be balanced by targeting either towards the same SOC. The algorithm built into the embedded microcontroller determines which cells need to be injected with extra charges, the amount of injection current, the duration of the injection time and the sequence of the injection.

At the beginning of each balancing cycle, all battery cell voltages are measured and the digitized voltages are sent to the computation unit (customized logic or micro processor based unit). The computation unit then determines how much extra charge each battery cell needs and sends commands to the switch matrix to open the associated switches at certain time and sequence to perform the active cell balancing. Soft-start inductor current ramp and soft-shutdown inductor current ramp is added in the command current to avoid the overstress of the switching devices and potential saturation of the magnetic components.

5.5 **System Control and Power Management**

The battery pack consists of three series connected battery modules. Each battery module consists of twelve series connected battery units which have four parallel connected battery cells ($= 2.3 \text{ Ah} \times 4$) in one unit, as shown in Figure 5.4. The total energy capacity of the battery pack consisting of three series-connected battery modules is $W = 1.09 \text{ kWh} (= 2.3 \text{ Ah} \times 4 \times 12 \times 3 \times 3.3 \text{ V})$. The dc voltage range is from 108 to 129.6 V (Assume working cell voltage is from 3.0 to 3.6 V).
Figure 5.4 One battery module in the box.

Figure 5.5 Control block diagram for the battery energy storage system
Figure 5.5 shows the control block diagram of the battery energy storage system. The whole control consists of three subcontrols: 1) central control; 2) bidirectional power flow control; 3) SOC balancing control.

The bidirectional power flow control is presented in Chapter 4. The SOC balancing control consists of cell-balancing control and module-balancing. The target of the cell-balancing control is to keep each of the 12-cell SOC values in a module (for example, SOC_{Ba1}, SOC_{Ba2}, ..., SOC_{Ba12}) equal to the mean SOC value of the corresponding module (SOC_{Ba}) shown in . Similarly, the target of module-balancing control is to keep each of the three module SOC values in a pack (SOC_{a}, SOC_{b}, ..., SOC_{c}) equal to the mean SOC value of the pack (SOC_{abc})

\[
\begin{align*}
\begin{bmatrix}
SOC_{Ba} \\
SOC_{Bb} \\
SOC_{Bc}
\end{bmatrix} &= \frac{1}{12} \begin{bmatrix}
SOC_{Ba1} + SOC_{Ba2} + \cdots + SOC_{Ba12} \\
SOC_{Bb1} + SOC_{Bb2} + \cdots + SOC_{Bb12} \\
SOC_{Bc1} + SOC_{Bc2} + \cdots + SOC_{Bc12}
\end{bmatrix} \\
SOC_{abc} &= \frac{1}{3} (SOC_{a} + SOC_{b} + SOC_{c})
\end{align*}
\]

\[
\begin{align*}
\begin{bmatrix}
SOC_{a} \\
SOC_{b} \\
SOC_{c}
\end{bmatrix} &= \begin{bmatrix}
SOC_{Ba1} + SOC_{Ba2} + \cdots + SOC_{Ba12} \\
SOC_{Bb1} + SOC_{Bb2} + \cdots + SOC_{Bb12} \\
SOC_{Bc1} + SOC_{Bc2} + \cdots + SOC_{Bc12}
\end{bmatrix} \\
SOC &= SOC_{a} + SOC_{b} + SOC_{c}
\end{align*}
\]

The central controller has three main inputs: \(P_{\text{ref_grid}}\) and \(Q_{\text{ref_grid}}\) commands from the grid and SOC estimation from the battery pack. When \(P_{\text{ref_grid}}\) is too large and beyond battery pack’s capability, SOC will take charge of the control. Otherwise, \(P_{\text{ref_grid}}\) will be taken as the control reference.

The inputs Max (SOC_{a, b, c}) and Min (SOC_{a, b, c}) of the central controller are used to limit the power in and out of the battery pack. In case the total SOC meets the power transferring requirement but the three battery modules are not balanced very well, then
the maximum power transferred from battery pack to grid is limited by \( \text{Min} \ (\text{SOC}_{a, b, c}) \) and the maximum power transferred from grid to battery pack is limited by \( \text{Max} \ (\text{SOC}_{a, b, c}) \). The inputs \( \text{Max} \ (\text{SOC}_{Ba1, \ldots, Ba12}), \text{Min} \ (\text{SOC}_{Ba1, \ldots, Ba12}), \text{Max} \ (\text{SOC}_{Bb1, \ldots, Bb12}), \text{Min} \ (\text{SOC}_{Bb1, \ldots, Bb12}), \text{Max} \ (\text{SOC}_{Bc1, \ldots, Bc12}), \text{Min} \ (\text{SOC}_{Bc1, \ldots, Bc12}) \) have the similar functions.

5.6 Experimental Results

This section shows the experimental results with the battery energy storage system at room temperature, which is around 20°C.

5.6.1 Battery Pack Charging and Discharging Waveforms

Figure 5.6 shows the experimental results when battery pack was repetitively charged to a SOC of 70% and discharged to a SOC of 30%. A wider window, for example, from 10% to 90%, may be used in an actual system. However, the lithium-ion batteries show longer lifecycle with a lower depth-of-discharge (DOD). The charging and discharging battery current is set at 9.2 A, which is equivalent to 1.0 C (= 9.2 A / 2.3 Ah / 4). The sampling rate of voltage and SOC is 2/s.
5.6.2 Effectiveness of the SOC Balancing Control

The SOC balancing control is to keep each of the twelve unit SOC values in a module equal to the mean SOC value of the corresponding module. In the experiment, each unit consists of four parallel connected cells except one unit is configured to have three parallel connected cells. Thus there is a 25% capacity mismatch inside the module.

Figure 5.7 shows the test results with SOC balancing and without SOC balancing. For the test without SOC balancing, all the twelve units are charged up to 100% SOC in the initial point. For 1 C discharging, the total time for discharging the module from 100% SOC to 0 % is limited by the unit consisting of three parallel connected cells, which is around 45 minutes. For 1 C charging, the total time for charging the module from 0% SOC to 100 % is limited by the unit consisting of three parallel connected cells, which is also about 45 minutes. For the testing with SOC balancing, the corresponding discharging and charging time are both 55 minutes. It can be concluded that the system with SOC balancing has 22% more capacity than the system without SOC balancing.
Figure 5.7 Experimental results of discharging and charging of one battery module. (a) Discharging without SOC balancing control. (b) Charging without SOC balancing control. (c) Discharging with SOC balancing control. (d) Charging with SOC balancing control.
In actual system, a SOC window between 30% and 70% may be used to extend battery cycle life time. For 1 C discharging without SOC balancing, the time for discharging the module from 70% SOC to 30% is around 18 minutes. The time for charging the module from 30% SOC to 70% is about 18 minutes. For the testing with SOC balancing, the corresponding discharging and charging time are both 24 minutes. It can be concluded that the system with SOC balancing has gained 33% more capacity than the system without SOC balancing when the SOC is between 30% and 70%. Without SOC balancing, lower capacity battery units in a battery module can be easily damaged with a higher DOD.

5.6.3 System Efficiency

![Figure 5.8 Experimental results of repetitively charging and discharging of the battery pack with SOC ranging between 30% and 70%.

Figure 5.8 Experimental results of repetitively charging and discharging of the battery pack with SOC ranging between 30% and 70%.

For 1 C charging and discharging, the relationship between battery pack voltage and SOC is shown in Figure 5.8. The arrows show the charging and discharging directions. The area 1 inside the curve is the relative losses when the battery pack is charged from 30% SOC to 70% SOC and discharged back to 30%. The losses consist of battery loss
and BMS loss. The round-trip efficiency is 96.5% for the battery pack. The overall round-trip efficiency for the battery energy storage system consisting of battery pack with associated BMS and bidirectional ac-dc converter is 92.6%.

5.7 Summary

In this chapter, a high-efficiency grid-tie lithium-ion battery based energy storage system is presented. The system consists of three subsystems, a LiFePO$_4$ battery pack and associated BMS, a bidirectional ac-dc converter, and the central control unit which controls the operation mode and grid interface of the energy storage system.

The designed BMS monitors and reports all battery cells parameters in the pack, these include cell voltage, temperature, and charging and discharging current. Based on these parameters, the BMS controller estimates the SOC of each battery cell in the pack by using the Coulomb counting plus an accurate open-circuit voltage model. The SOC information is then used to control the isolated bidirectional dc-dc converter based active cell balancing circuits to mitigate the mismatch among the series connected cells. The SOC and SOH information is also used by the central control unit to determine the operating mode of the energy storage system. Using the proposed SOC balancing technique, the entire battery storage system has demonstrated more capacity than the system without SOC balancing. Under the charging condition from 0 to 100% SOC and discharging condition from 100% SOC to 0, the use of SOC balancing technique has 22% more capacity. Under the charging condition from 30% to 70% SOC and discharging condition from 70% to 30% SOC, the use of SOC balancing technique has 33% more capacity.

The overall round-trip efficiency for the battery energy storage system consisting of battery pack with associated BMS and bidirectional ac-dc converter is 92.6%.
Chapter 6  Conclusions and Future Work

6.1 Summary

This dissertation proposed a high-efficiency grid-tie lithium-ion battery based energy storage system. The system consists of three subsystems, a LiFePO₄ battery pack and associated BMS, a bidirectional ac-dc converter, and the central control unit which controls the operation modes and grid interface of the energy storage system. The BMS controller monitors the parameters of each battery cell and applies the charge equalization circuits to mitigate the mismatch among the series connected battery cells. The bidirectional ac-dc converter works as the interface between the battery pack and the ac grid, which needs to meet the requirements of bidirectional power flow capability and to ensure high power factor and low THD as well as regulate the dc side power regulation. The central control unit communicates with the battery management system and bidirectional ac-dc converter. It combines the SOC information and power command coming from the grid side to control the bidirectional power flow between ac grid and dc battery energy storage.

The following conclusions are drawn from the work.

1) Dual-buck converter based single-phase bidirectional ac-dc converter is proposed. The converter exhibits two distinct merits: first, there is no shoot-through issue because no active power switches are connected in series in each phase leg; second, the reverse recovery dissipation of the power switch is greatly reduced because there is no freewheeling current flowing through the body diode of power switches.

- A new SPWM scheme by using split SPWM as the main scheme and joint SPWM as the supplementary scheme for the zero-crossing region is proposed. On one hand, since split SPWM is utilized as the main scheme, conduction and switching losses are relatively low. On the other hand, because joint SPWM is employed for the zero-crossing region, the ac current becomes continues.
The utilization of the magnetic components is improved by employing different coupled inductor structures. One is employing one coupled inductor in series with small inductors and the other one is utilizing two coupled inductors in series. Overall, the implemented converter efficiency peaks at 97.8% at 50-kHz switching frequency for both rectifier and inverter modes.

2). To better utilize the dc bus voltage and eliminate the two dc bus capacitors, a novel bidirectional ac-dc converter is proposed by replacing the two-capacitor leg of the dual-buck converter based single-phase bidirectional ac-dc converter with a two-switch leg. The novel bidirectional ac-dc converter keeps the merits of the dual-buck converter based bidirectional ac-dc converter. Meanwhile the two large dc bus capacitors and related voltage-balancing control are eliminated.

The utilization of the magnetic components is improved by integrating transformers and inductors on the same core. Two different structures of magnetic integration are presented. One is employing one coupled inductor in series with small inductors and the other one is utilizing two coupled inductors in series.

Three novel three-phase bidirectional ac-dc converter topologies are proposed. They all preserve the merits of the novel single-phase bidirectional ac-dc converter with free of shoot through problems.

3). In order to control the bidirectional power flow and at the same time stabilize the system in mode transition, a unified digital controller is proposed.

The power stage small-signal model is derived for the dual-buck converter based single-phase bidirectional ac-dc converter.

Based on the small-signal model, an admittance compensator along with a QPR controller is adopted to allow smooth startup and elimination of the steady-state error over the entire load range.

The proposed QPR controller is designed and implemented with a digital controller. Then the coefficients of the digital controller are truncated into certain word length binary representation, so as to be fit to the numbers of bits available to the FPGA for variables and constants.
The entire system has been simulated in both PSIM and Simulink and verified with hardware experiments. Small transient currents are observed with the power transferred from rectifier mode to inverter mode at peak current point and also from inverter mode to rectifier mode at peak current point.

4) A BMS is designed to monitor and balance each battery cell in the pack.
   - The designed BMS monitors and reports all battery cells parameters such as cell voltage, temperature, and charging and discharging current. Based on these parameters, the BMS controller estimates the SOC of each battery cell in the battery pack by using the Coulomb counting plus an accurate open-circuit voltage model.
   - The SOC information is used to control the isolated bidirectional dc-dc converter based active cell balancing circuits to mitigate the mismatch among the series connected cells. The SOC and SOH information is also used by the central control unit to determine the operating mode of the energy storage system.

Using the proposed SOC balancing technique, the entire battery storage system has demonstrated more capacity than the system without SOC balancing. Under the charging condition from 0 to 100% SOC and discharging condition from 100% SOC to 0, the use of SOC balancing technique has 22% more capacity. Under the charging condition from 30% to 70% SOC and discharging condition from 70% to 30% SOC, the use of SOC balancing technique has 33% more capacity. The round-trip efficiency is 96.5% for the battery pack. The overall round-trip efficiency for the battery energy storage system consisting of battery pack with associated BMS and bidirectional ac-dc converter is 92.6%.

6.2 Future Work

(1) A battery energy storage system that contains a single-phase bidirectional ac-dc converter tends to inject or draw an ac ripple current at twice the ac frequency. Although the battery current does not change the direction, such a ripple current may shorten battery life span. One approach is to modify the single-phase bidirectional ac-dc
converter topology to reduce the amplitude of the ac ripple current. Another approach is to add an additional bidirectional dc-dc converter stage to smooth the ac ripple current.

(2) A unified current controller is adopted to control the bidirectional power flow and at the same time stabilize the system in mode transition. A voltage control scheme needs to be developed for voltage mode charging or discharging when the SOC of the battery pack reaches 0% or 100%.

(3) When the grid is abnormal, the microgrid formed by the battery energy storage system needs to disconnect from the main grid while supporting critical loads. A smooth transitioning control scheme needs to be developed and further investigated to offer the battery energy storage system the capability to switch between grid-tie and islanding modes.
References


